



Warsaw University of Technology

The Faculty of Automotive
and Construction Machinery Engineering

Institute of Machine Design Fundamentals

Department of Mechanics

<http://www.ipbm.simr.pw.edu.pl/>



Theory of Machines and Automatic Control

Winter 2017/2018

Lecturer: Sebastian Korczak, PhD, Eng.

Theory of Machines and Automatic Control

Winter 2017/2018

Field of studies: Electric and Hybrid Vehicle Engineering (full-time)

form of studies: 30 hrs lecture, 15 hrs project class

ECTS: 4

Lecture: Tuesdays at 8:15 (room 3.3)

**Projects: Wednesdays at 9:15 (room 3.8)
1st meeting on 8th November**

Lecturer: Sebastian Korczak, PhD, Eng.

room: 2.8b

e-mails: sebastian.korczak@simr.pw.edu.pl, admin@myinventions.pl

consultations: Tuesdays at 10:00-11:00 and Thursdays at 12:00-13:00

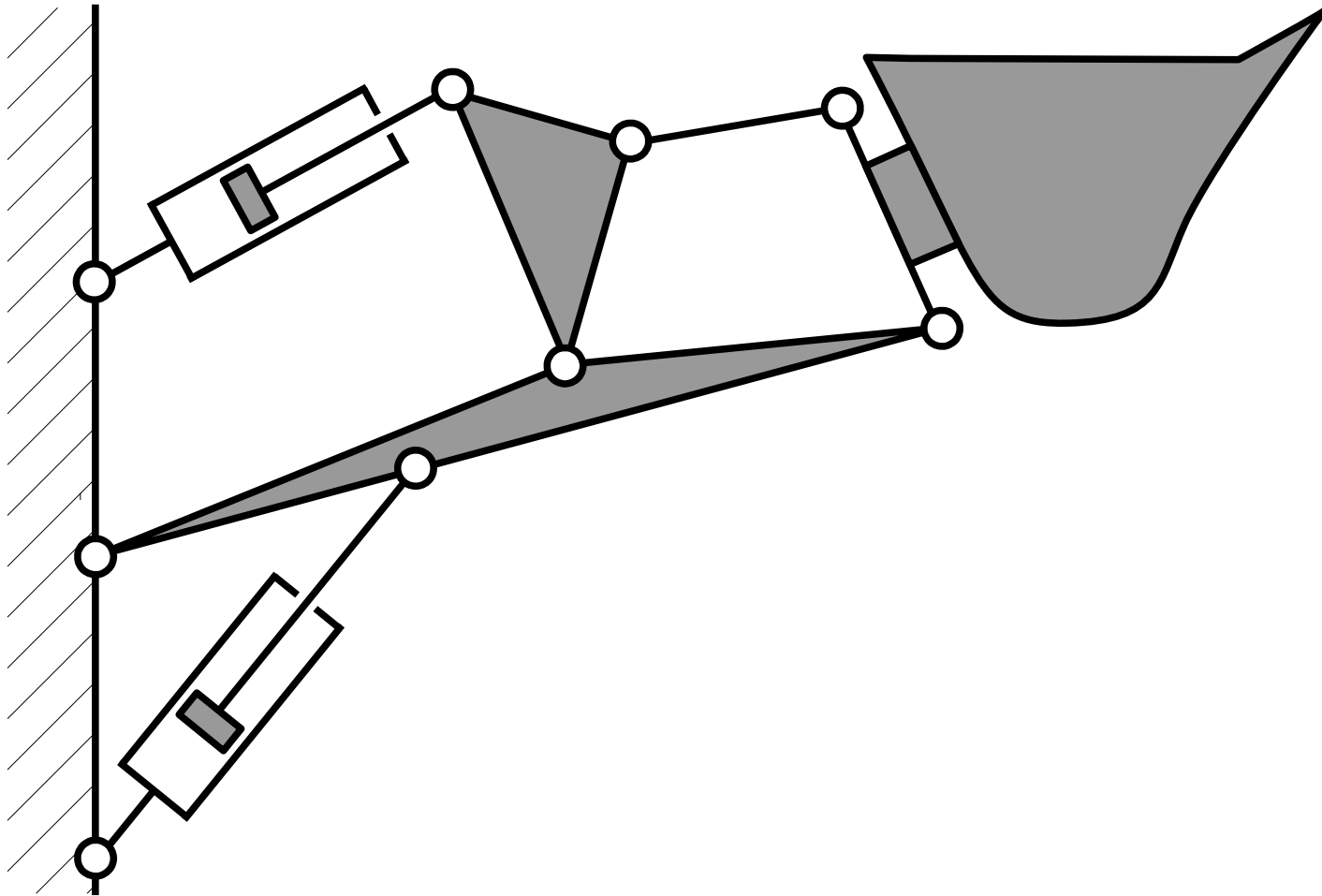
website with materials and marks: <http://myinventions.pl/lectures/>

Lecture 2

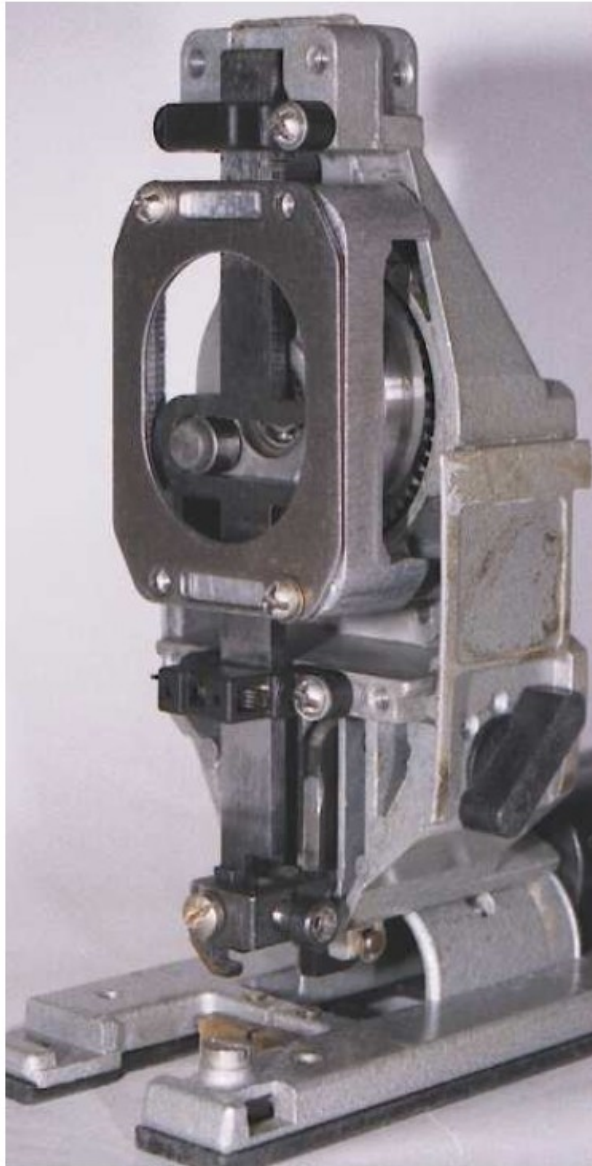
Structural classification, velocities in planar mechanisms.

Materials license: only for education purposes of Warsaw University of Technology students.

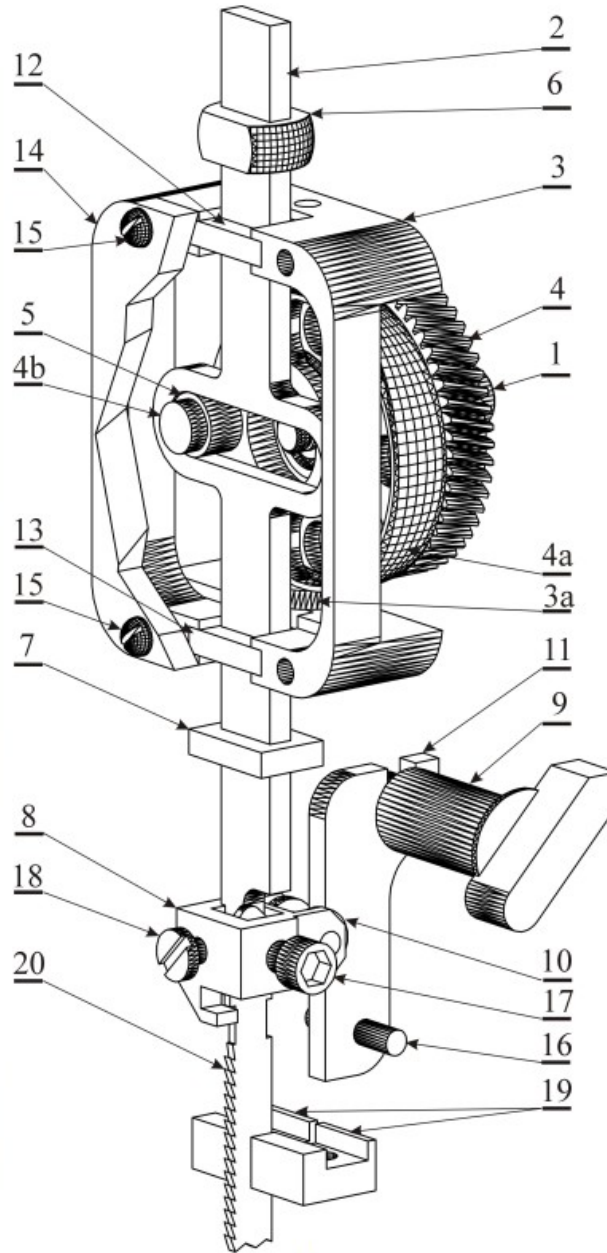
Starting examples



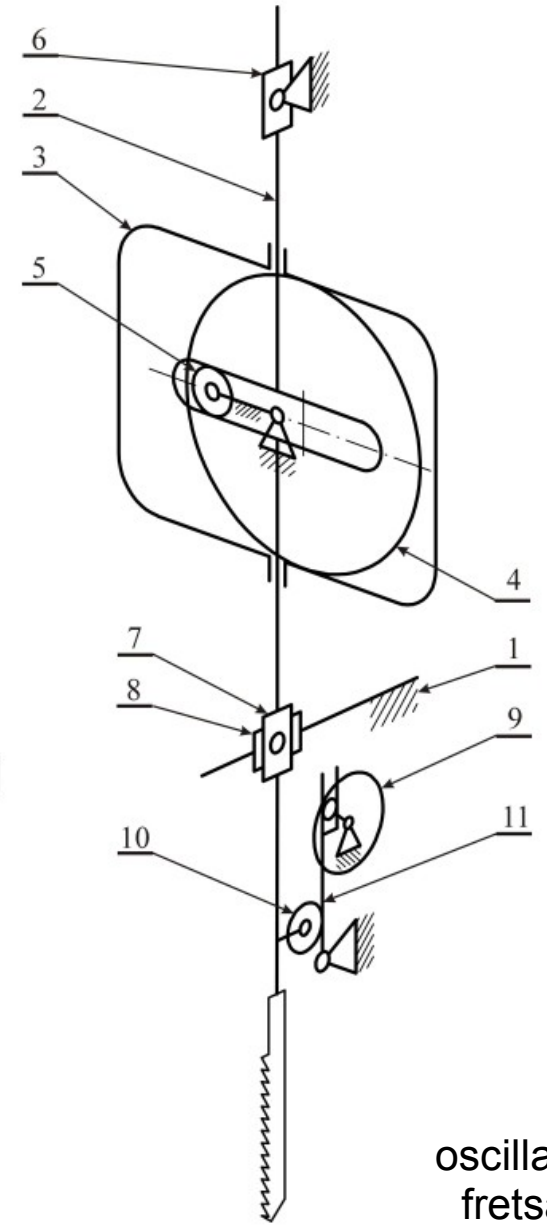
Starting examples



a



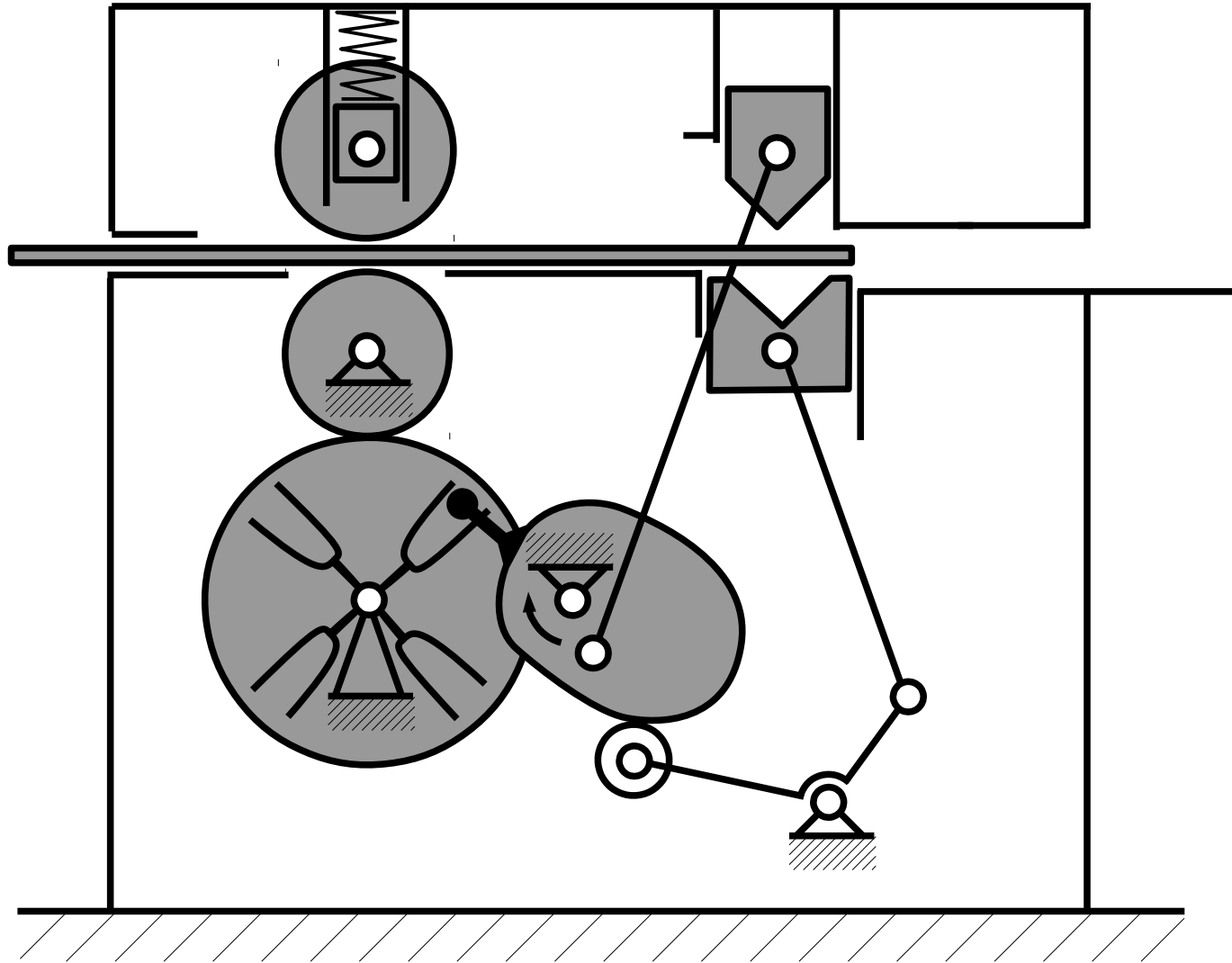
b



oscillatory
fretsaw

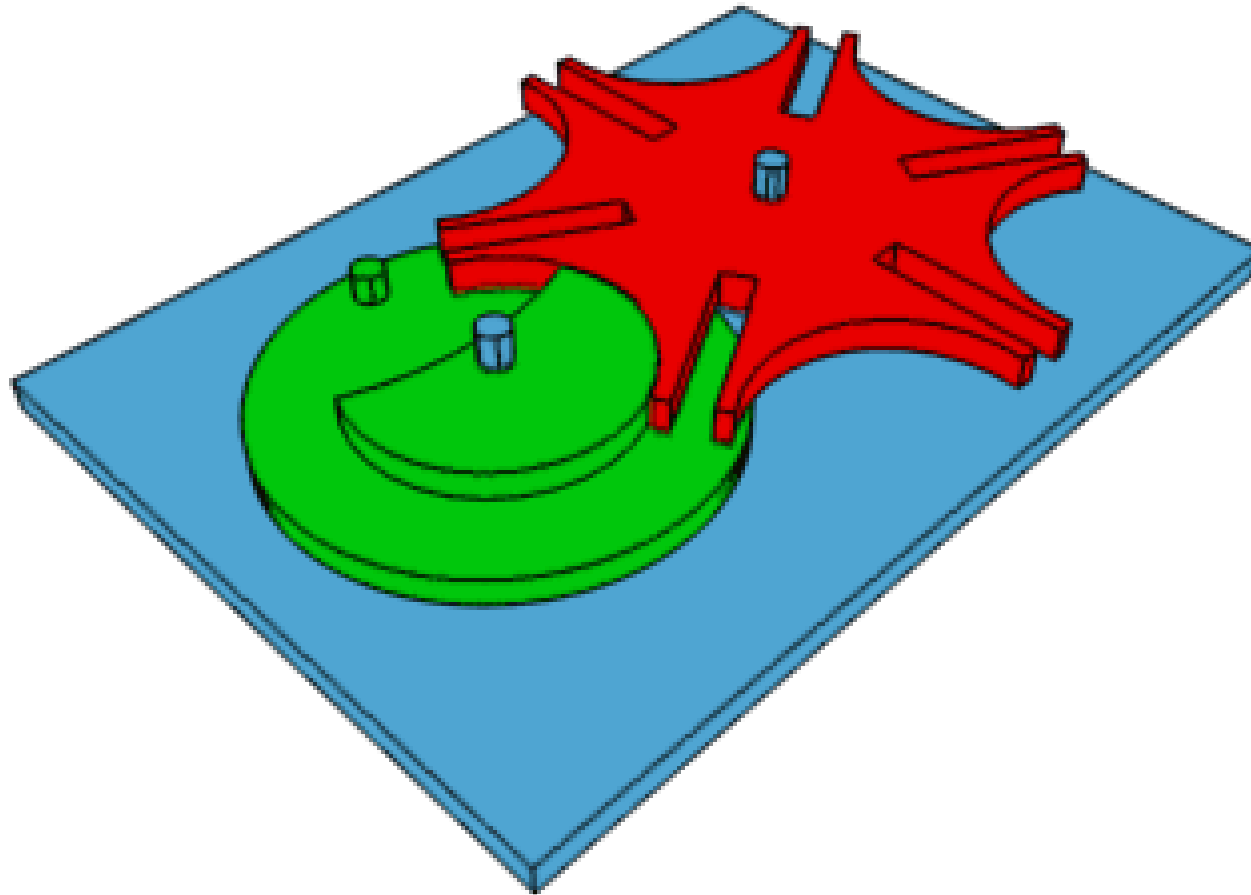
c

Starting examples



Starting examples

Geneva drive (Maltese cross)



Classification of kinematic chains

Simple kinematic chain – every member has maximum two kinematic pairs.

Complex kinematic chain – at least one member has three kinematic pairs.

Classification of kinematic chains

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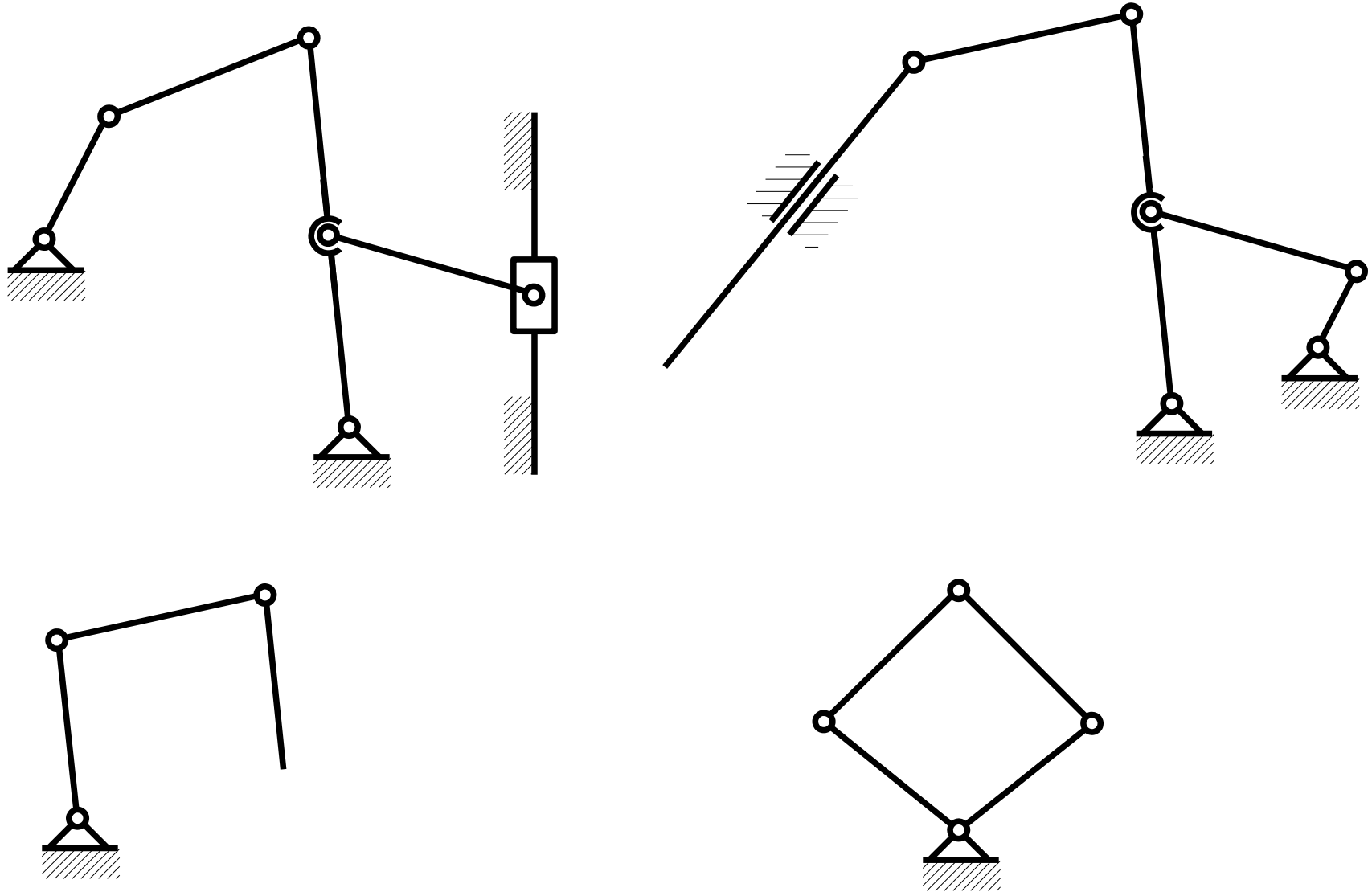
Complex kinematic chain – at least one member has three kinematic pairs.

Open kinematic chain – at least one member has only one kinematic pair.

Closed kinematic chain – every member has minimum two kinematic pairs.

Classification of kinematic chains

Examples



Structural classification of mechanisms

Structural group – the simplest part of mechanism that has zero mobility.

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Planar mechanism with only 5th class pairs: $F = 3n - 2p_5 = 0$

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$$\frac{p_5}{n} = \frac{3}{2} = \frac{6}{4} = \frac{9}{6} = \dots$$

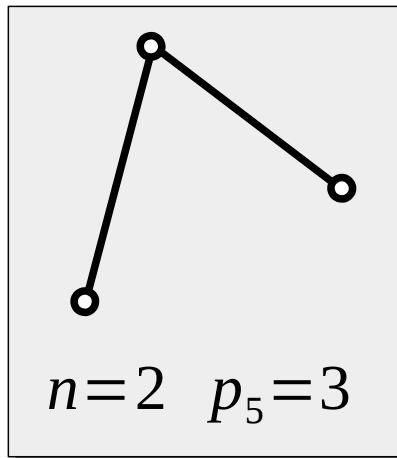
Structural classification of mechanisms

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Ind structural
group



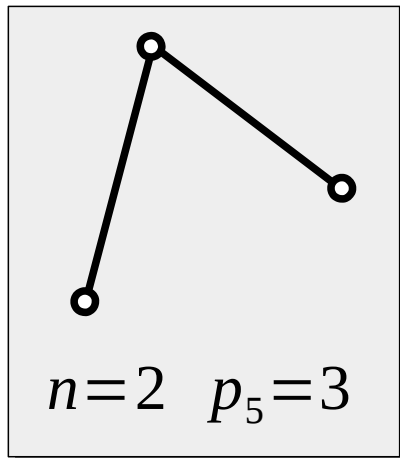
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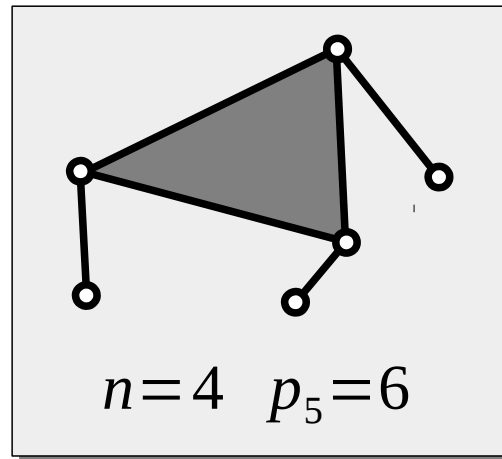
Planar mechanism with only 5th class pairs: $F = 3n - 2p_5 = 0$

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IInd structural group



IIIrd structural group



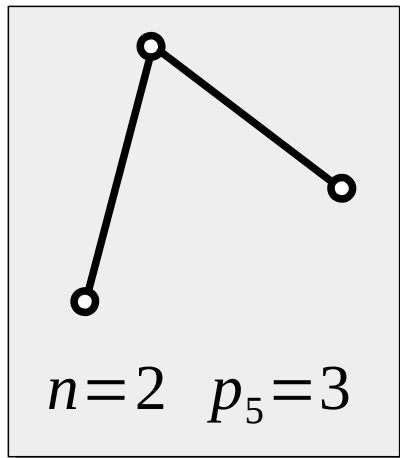
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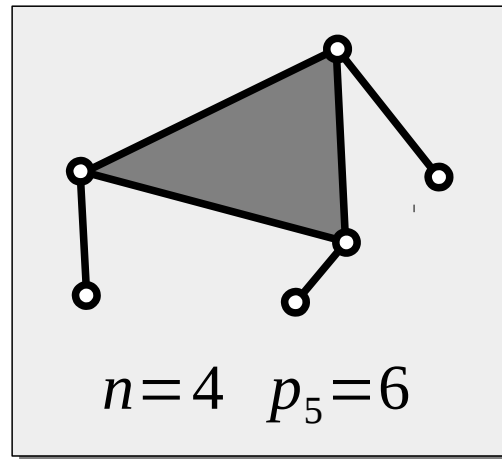
Planar mechanism with only 5th class pairs: $F = 3n - 2p_5 = 0$

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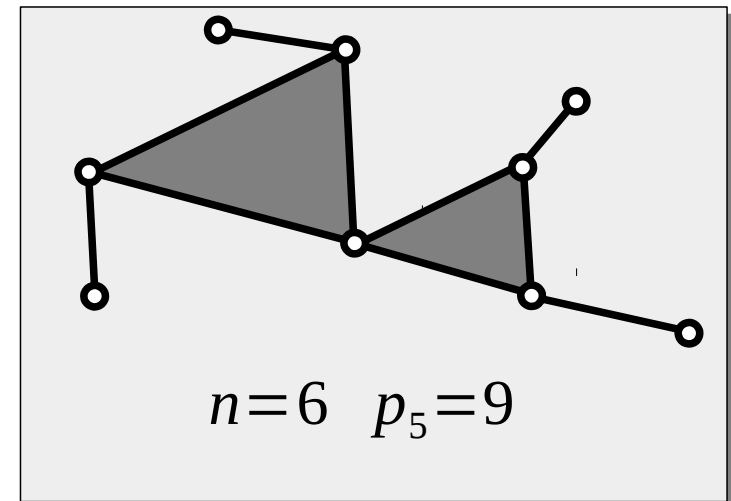
IInd structural group



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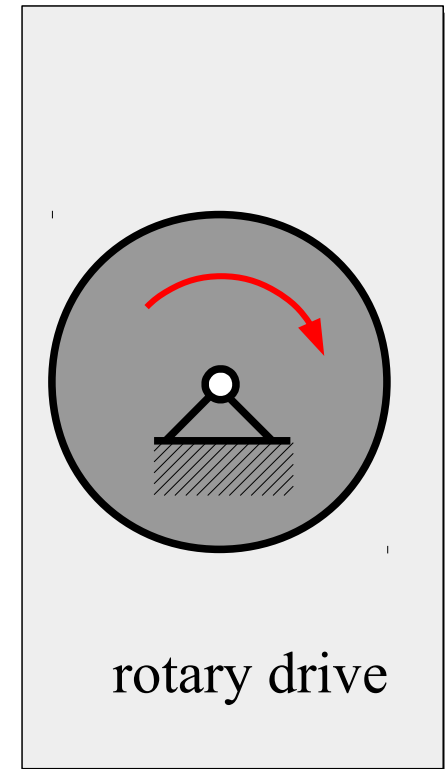
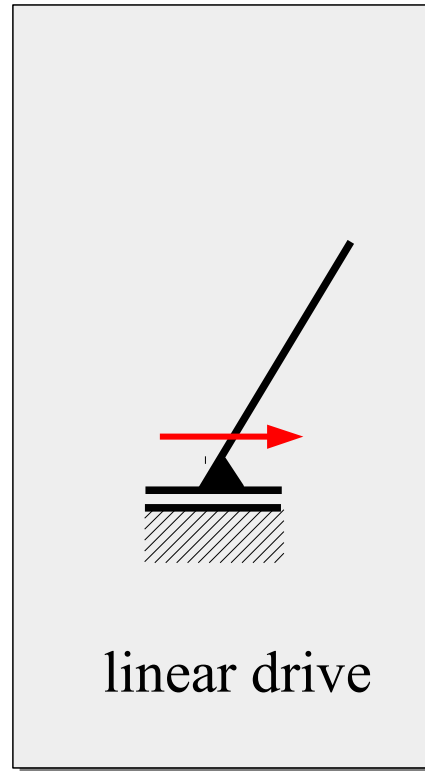
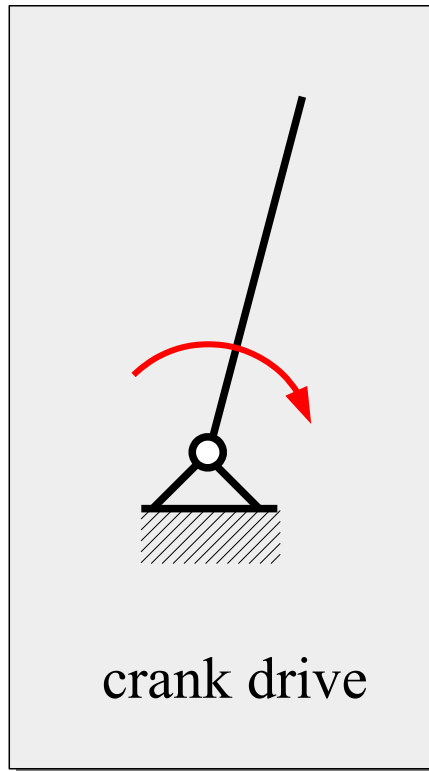
IVth structural group



Structural classification of mechanisms

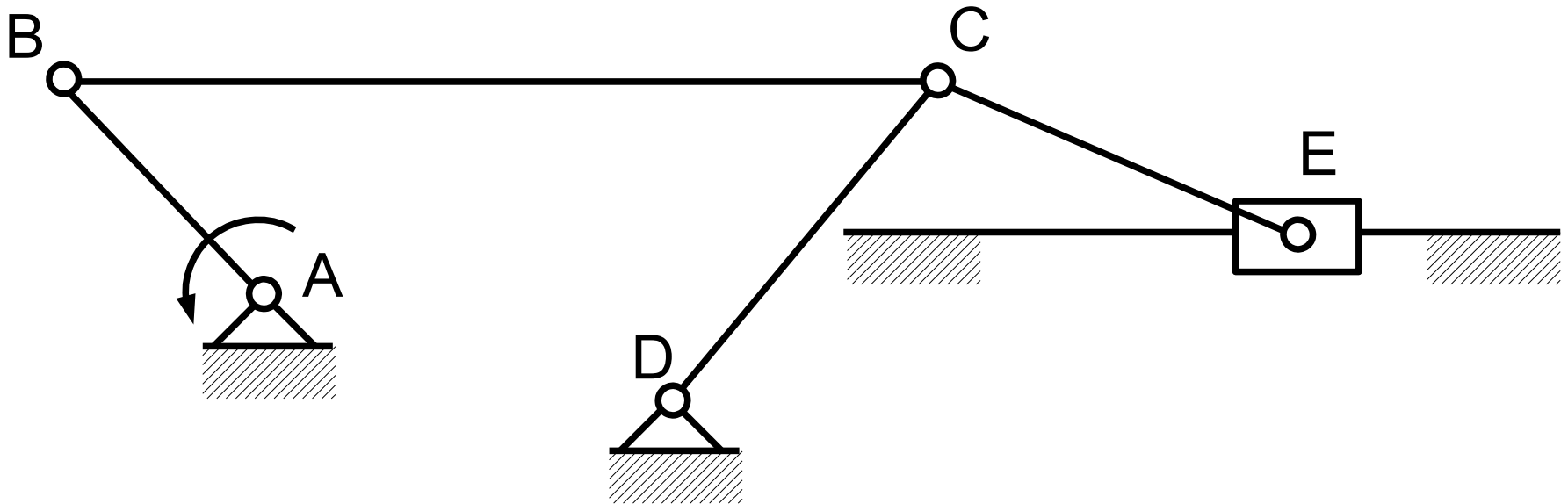
Ist structural group – drive

$$n=1 \quad p_5=1 \quad + \text{ drive}$$



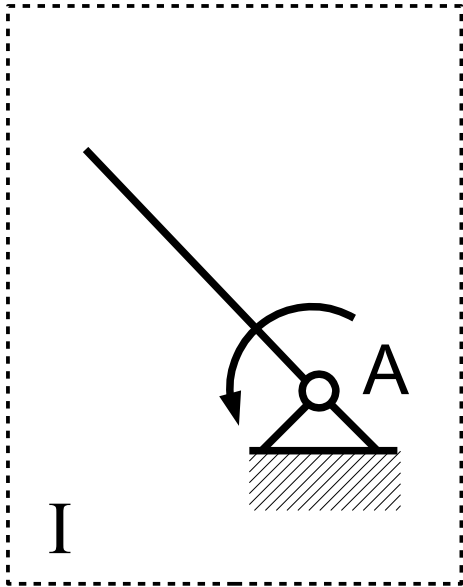
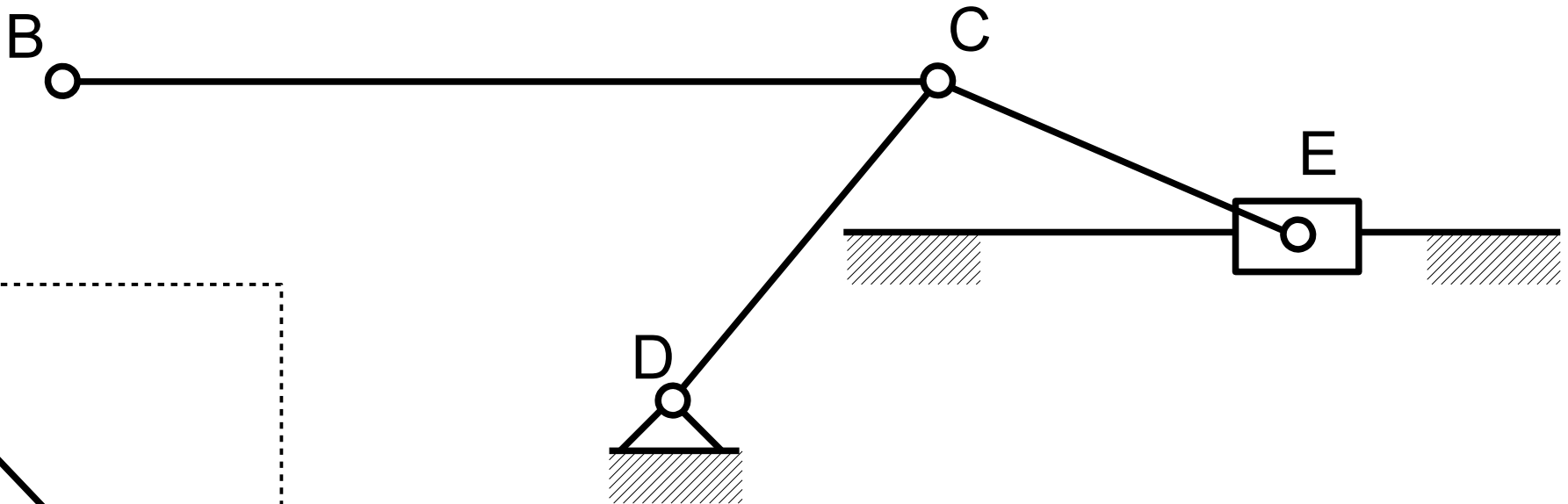
Structural classification of mechanisms

Example



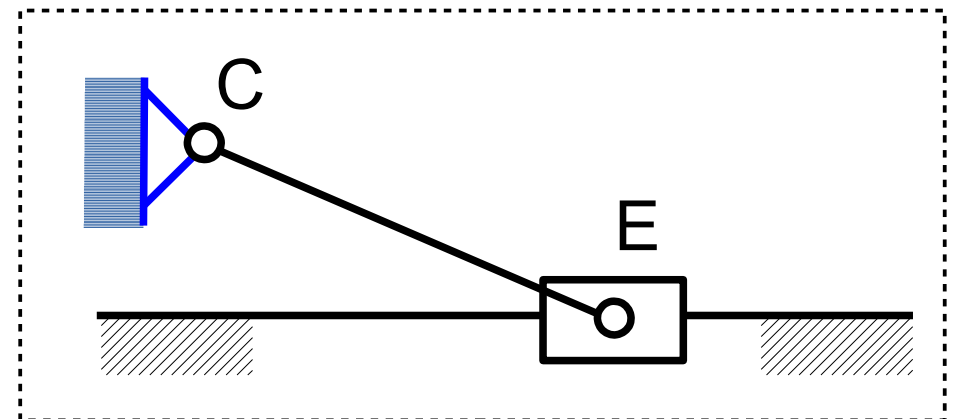
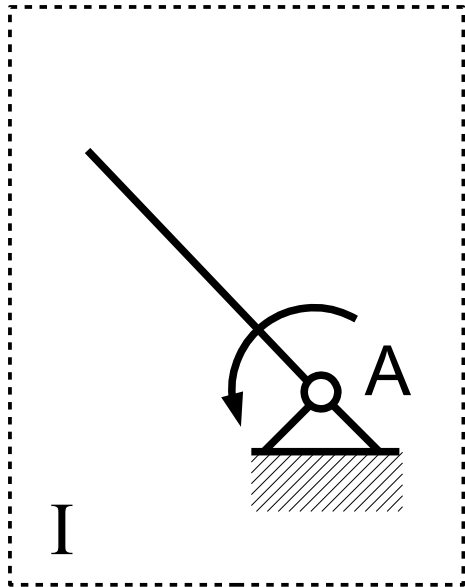
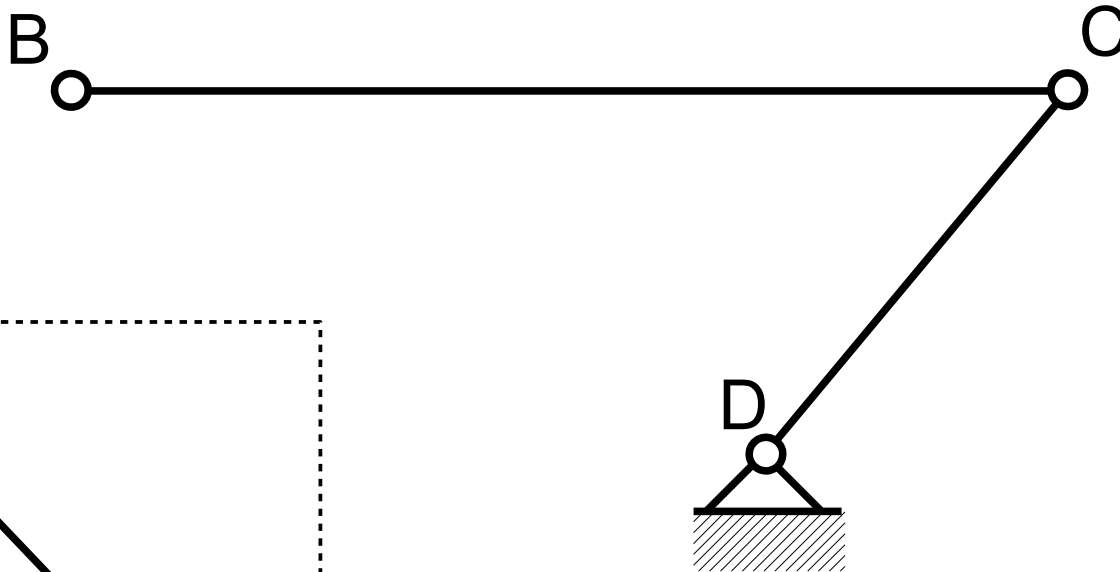
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Example



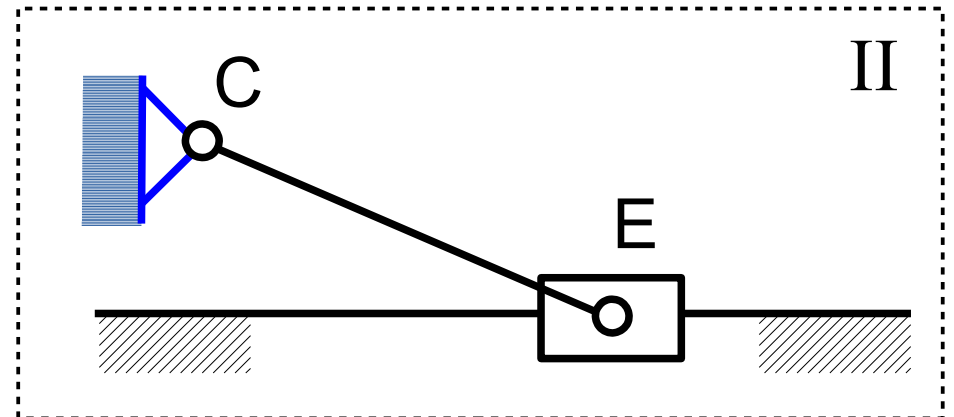
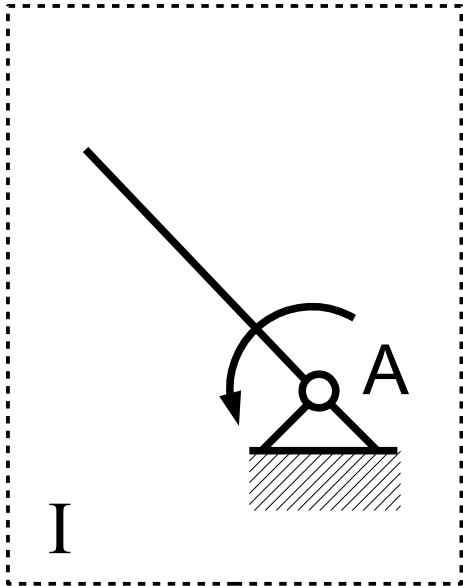
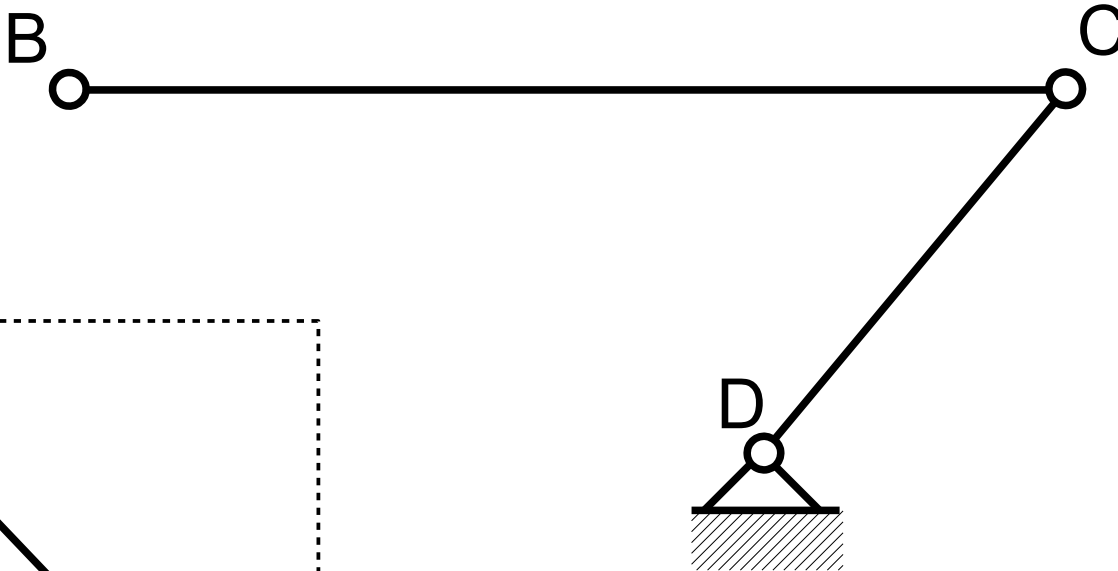
Structural classification of mechanisms

Example



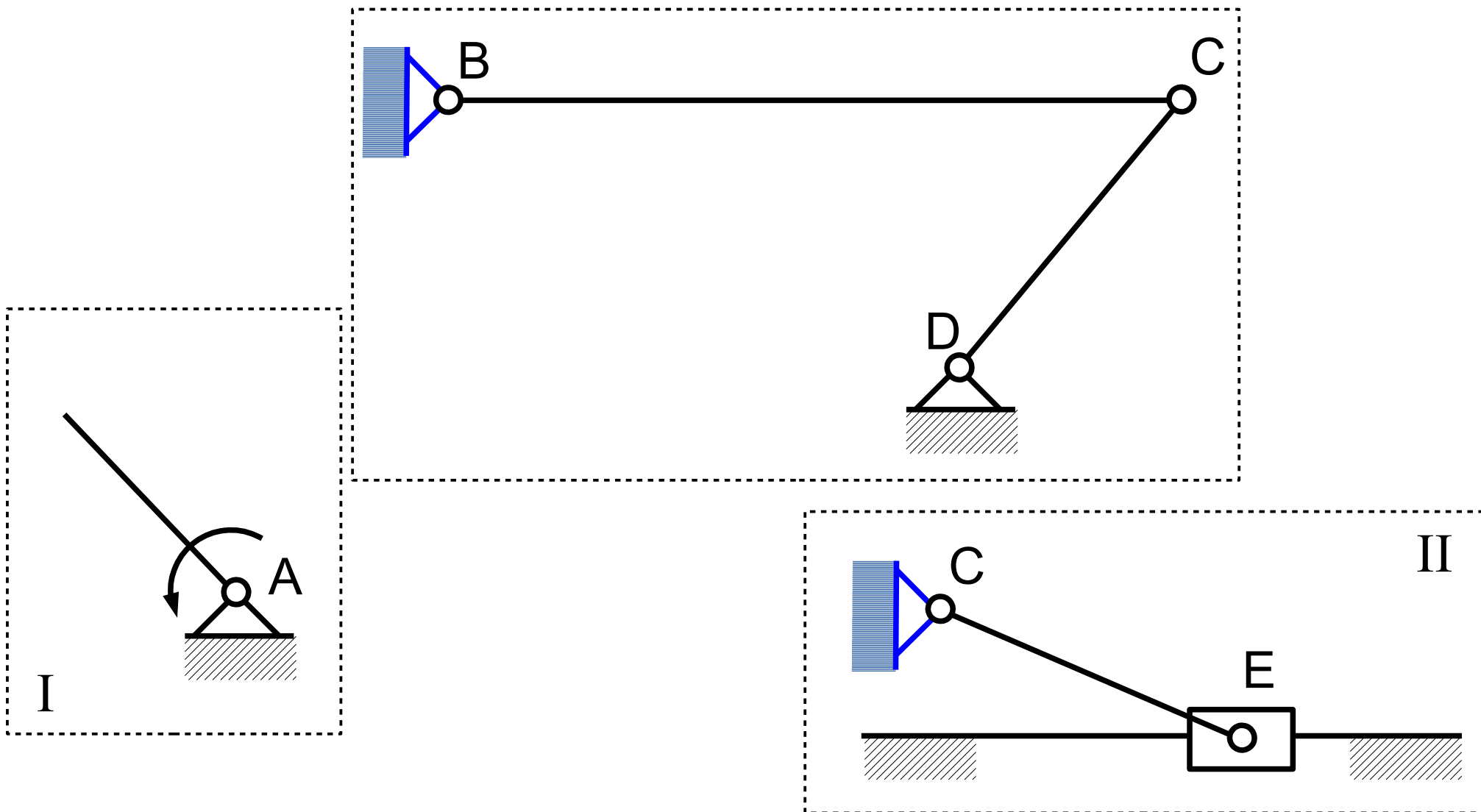
Structural classification of mechanisms

Example



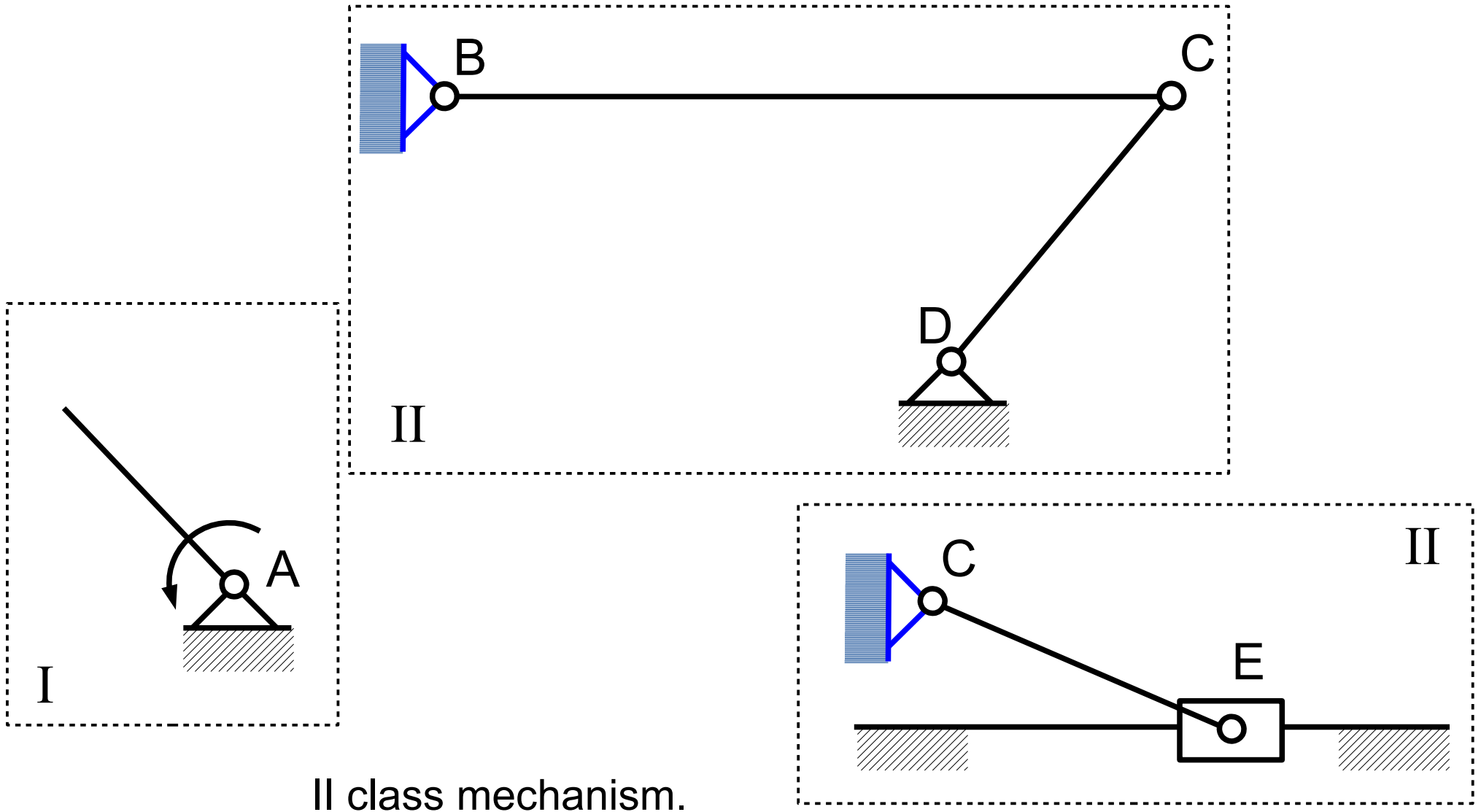
Structural classification of mechanisms

Example



Structural classification of mechanisms

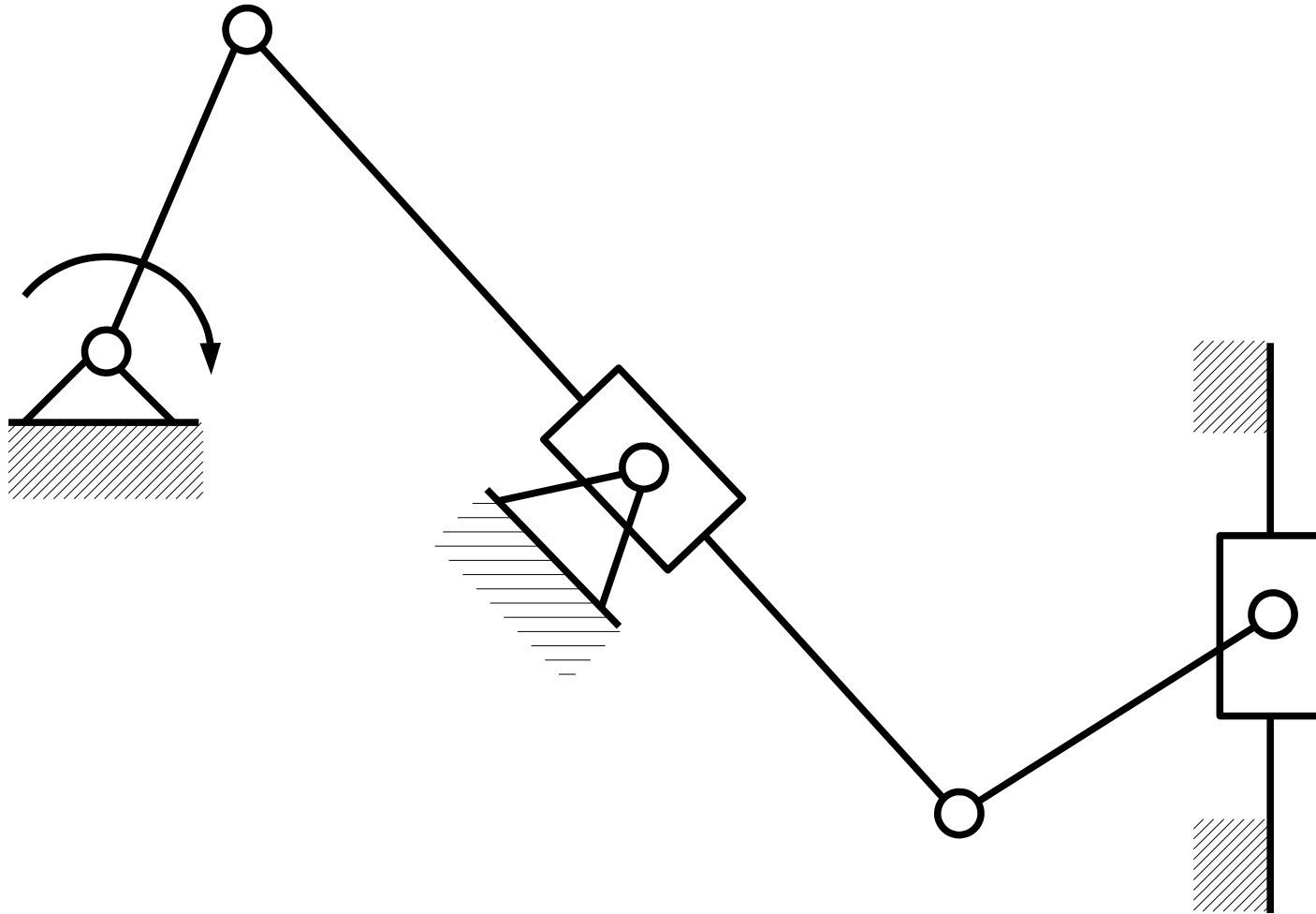
Example



II class mechanism.

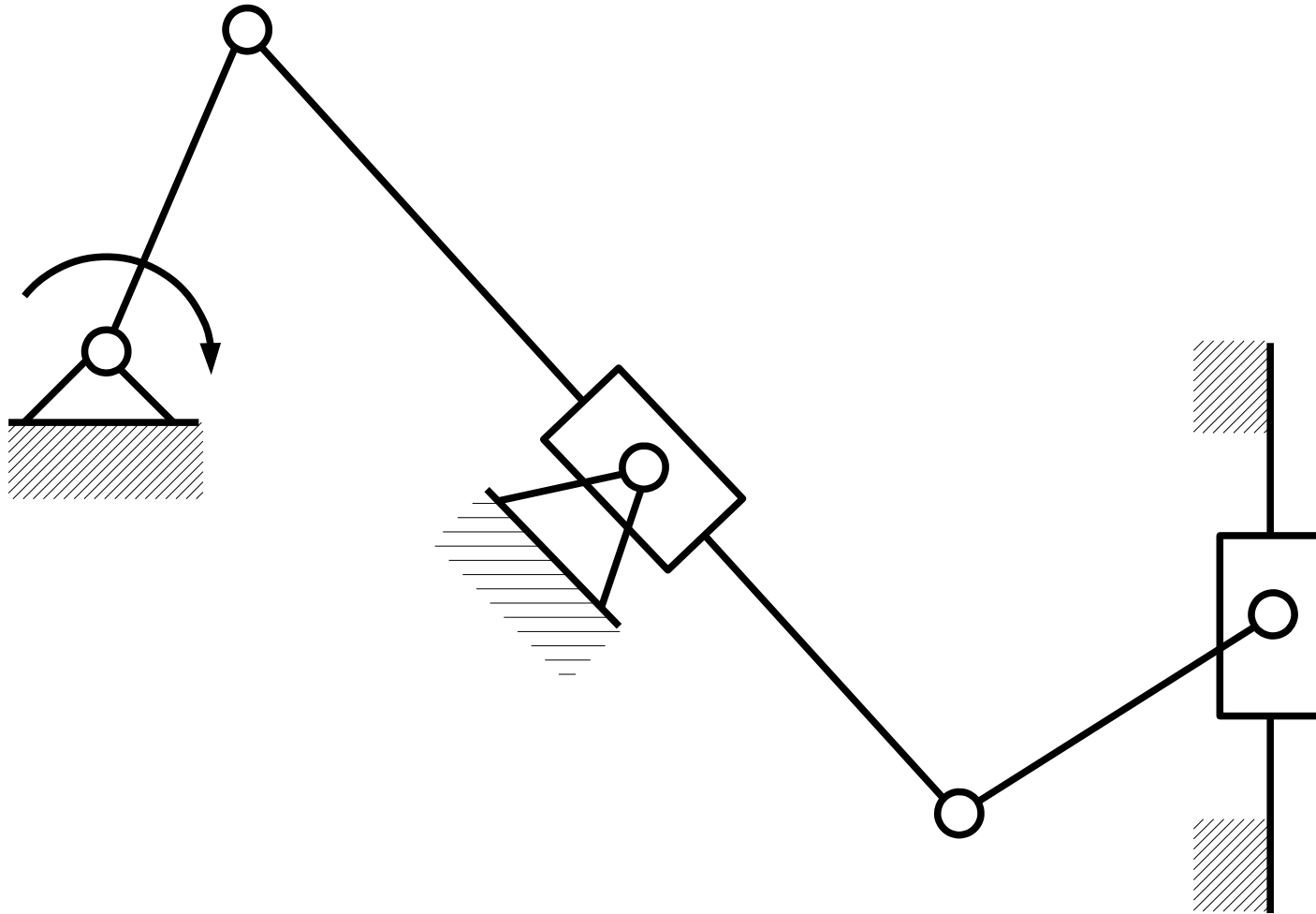
Structural classification of mechanisms

2nd Example



Structural classification of mechanisms

2nd Example



Kinematics of mechanisms

Kinematic analysis of a mechanism – determination of velocities and accelerations of selected mechanism members' points at considered configuration. Mechanism structure must be given (geometry of members, kinematic pairs) and drive method must be known.

Methods of velocities and acceleration determination

Graphical methods

- velocity projection method,
- instantaneous center of rotation method,
- instantaneous center of acceleration method,
- method of rotated velocities,
- velocity decomposition method,
- acceleration decomposition method,
- velocity scheme method,
- accelerations scheme method.

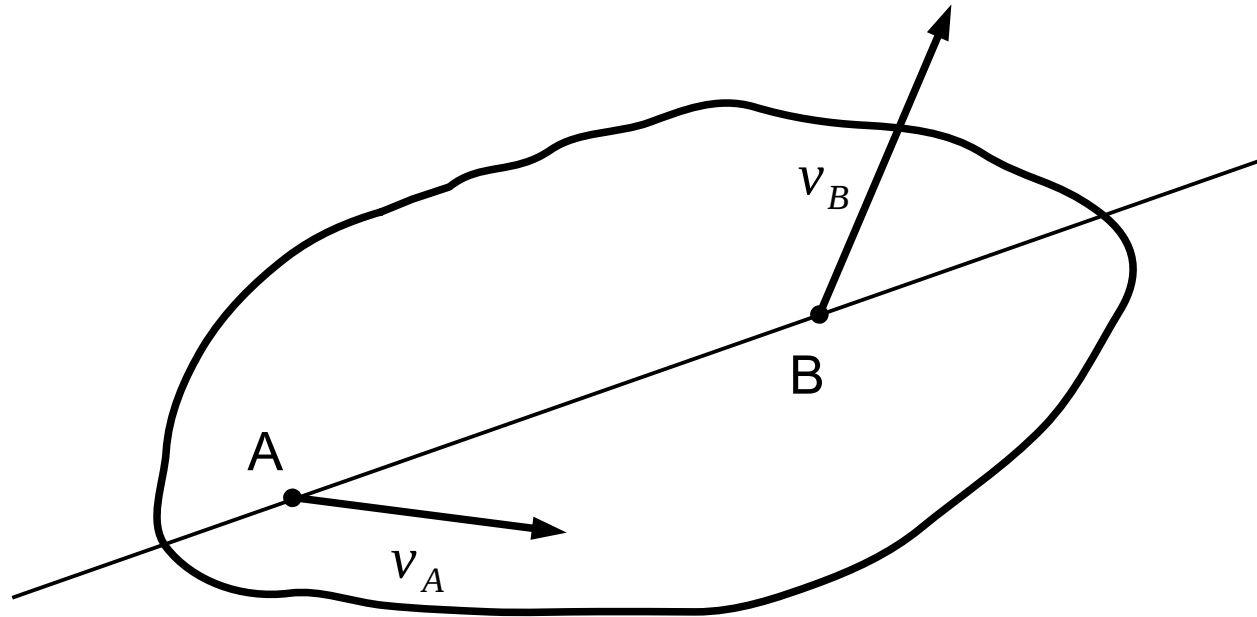
Analytical method

Methods of velocities and acceleration determination

	Graphical methods	Analytical method
advantage	<ul style="list-style-type: none">• better understanding of mechanism motion,• analysis of very complicated mechanisms,• computers not needed,	<ul style="list-style-type: none">• functions of configuration as a solution,• analysis of very complicated mechanisms,
disadvantage	<ul style="list-style-type: none">• great workload,• needs to repeat graphs for every configuration,• graphical errors.	<ul style="list-style-type: none">• computer needed for complicated mechanisms,• complicated systems of equations to solve,• solution interpretation may be complicated.

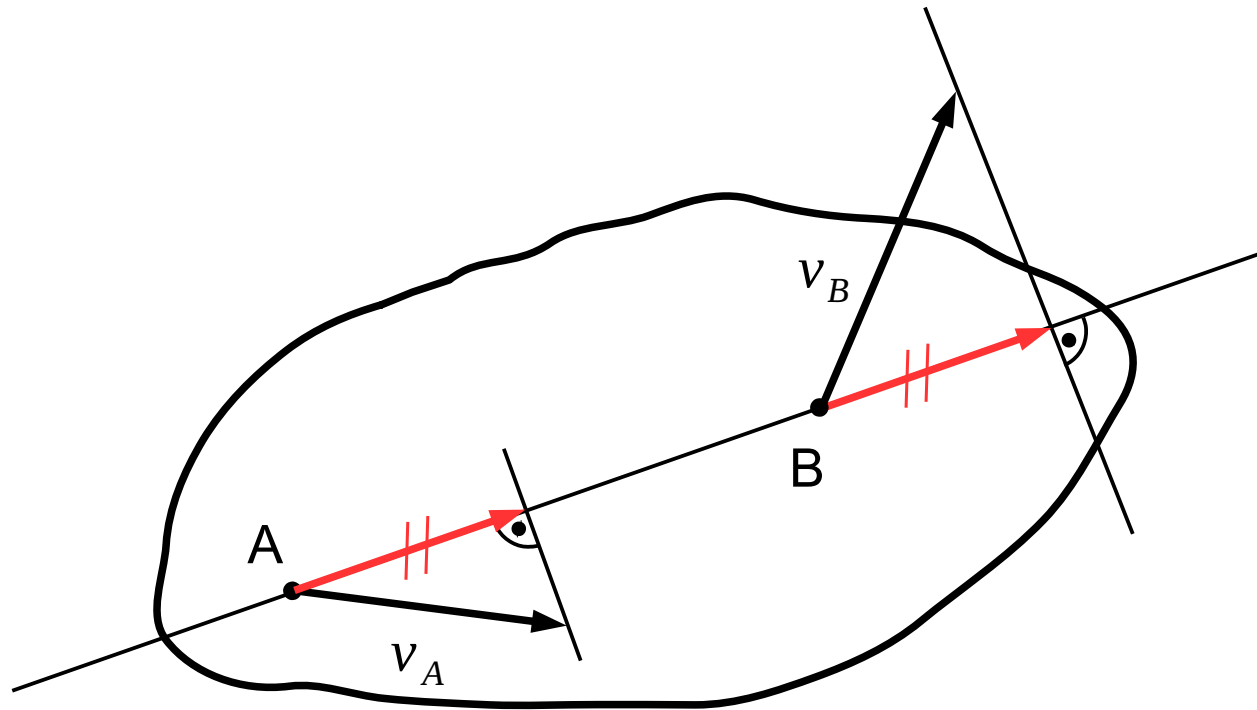
Velocity projection method

Projections of velocities of two rigid body's points onto common line are equal.



Velocity projection method

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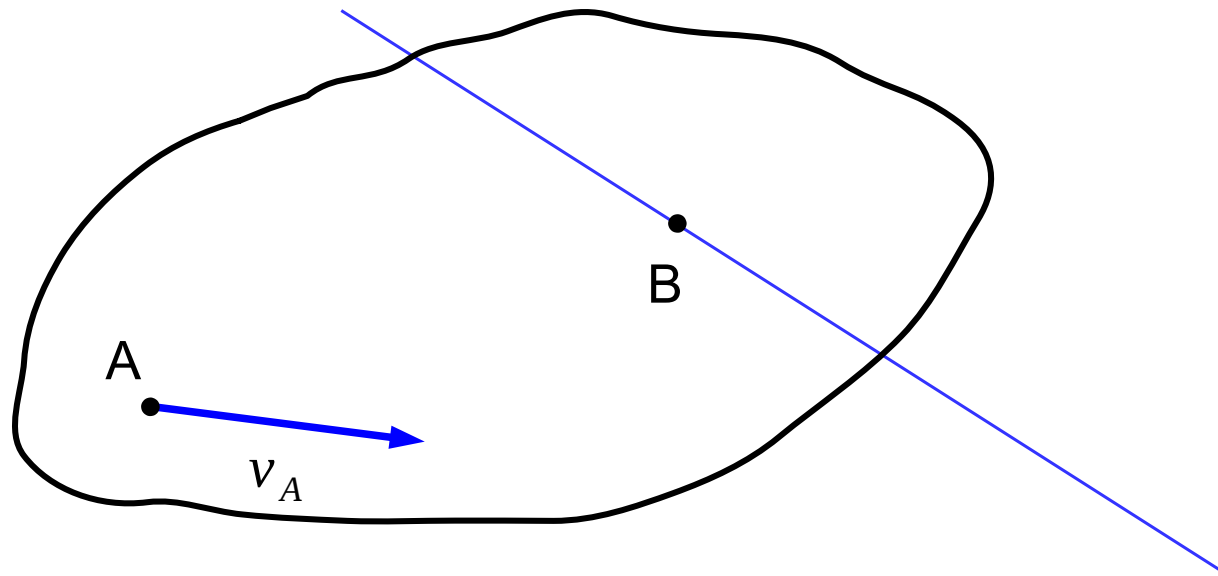


Velocity projection method

Example

Given: v_A and direction of v_B

Searched: v_B

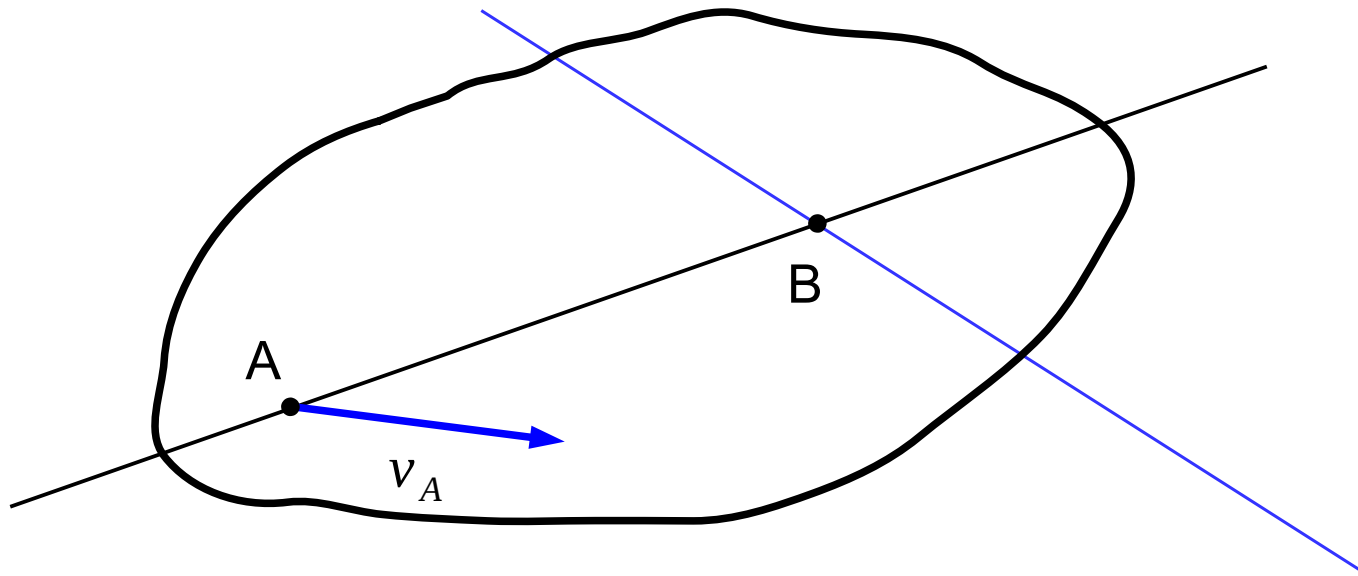


Velocity projection method

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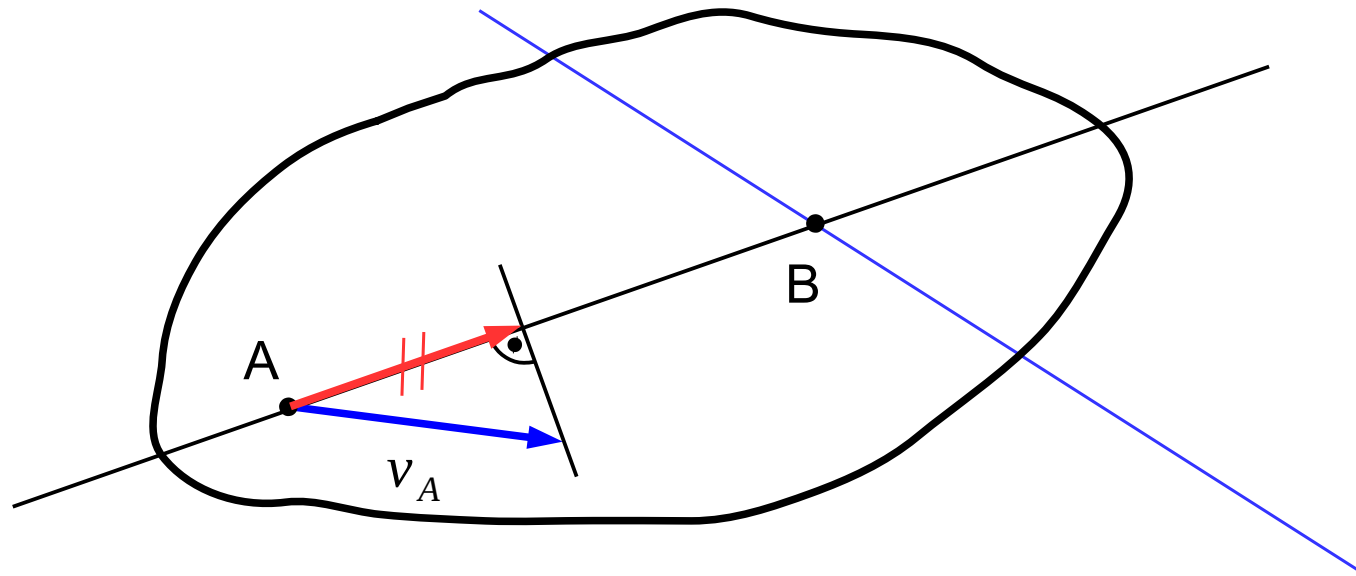


Velocity projection method

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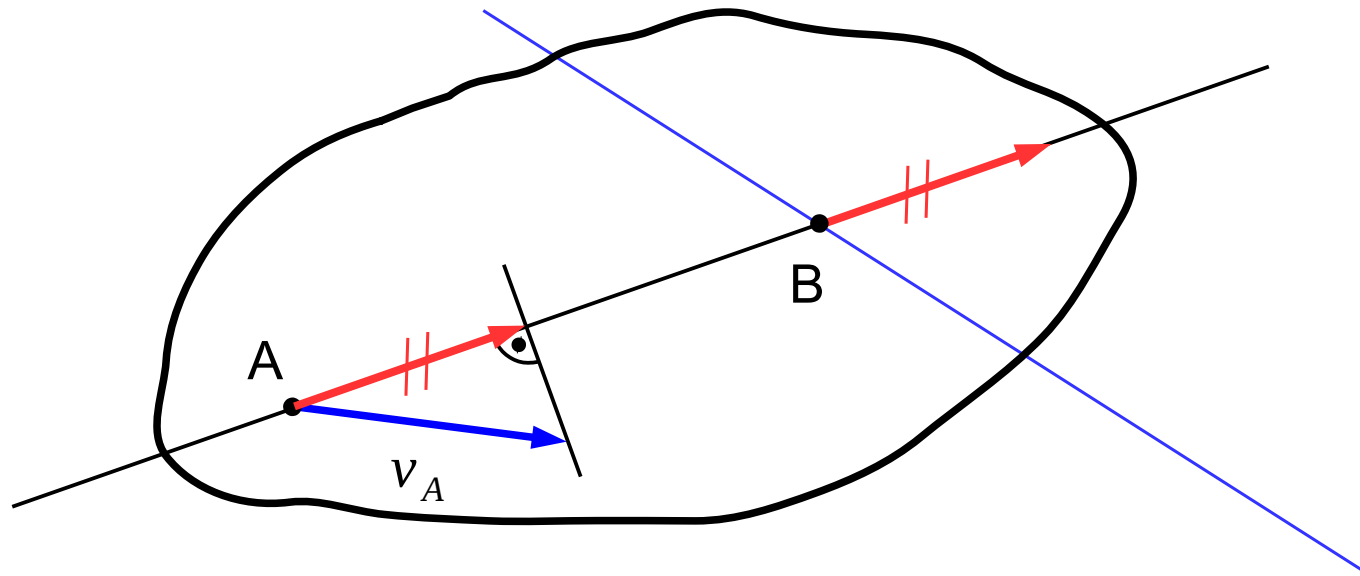


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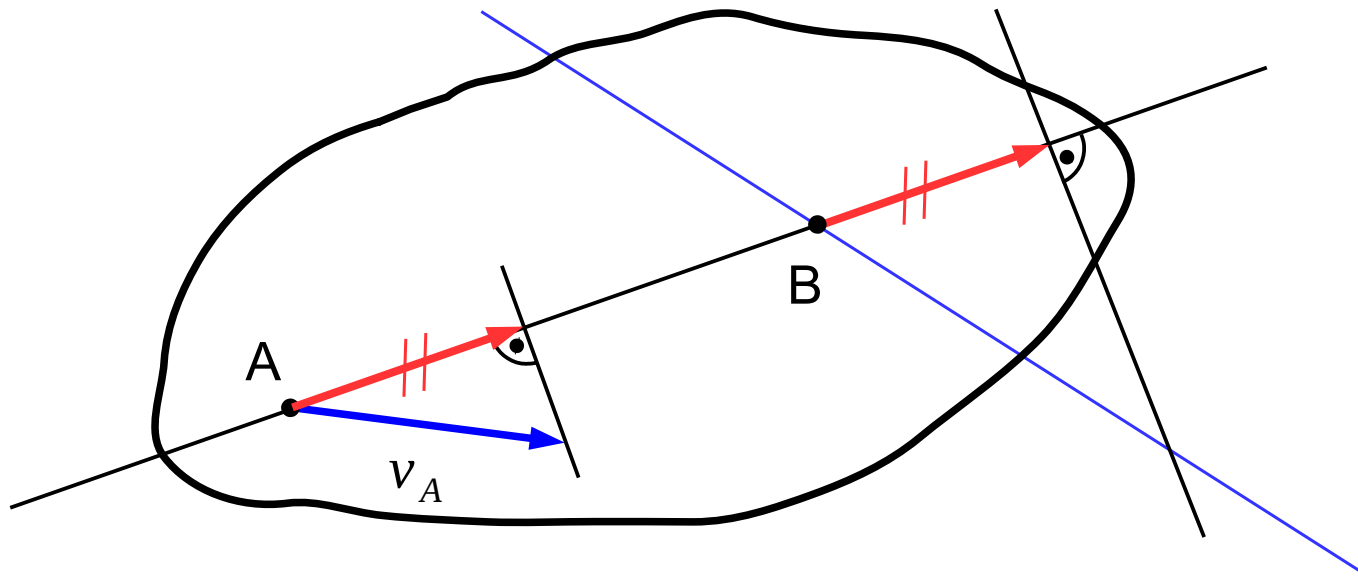


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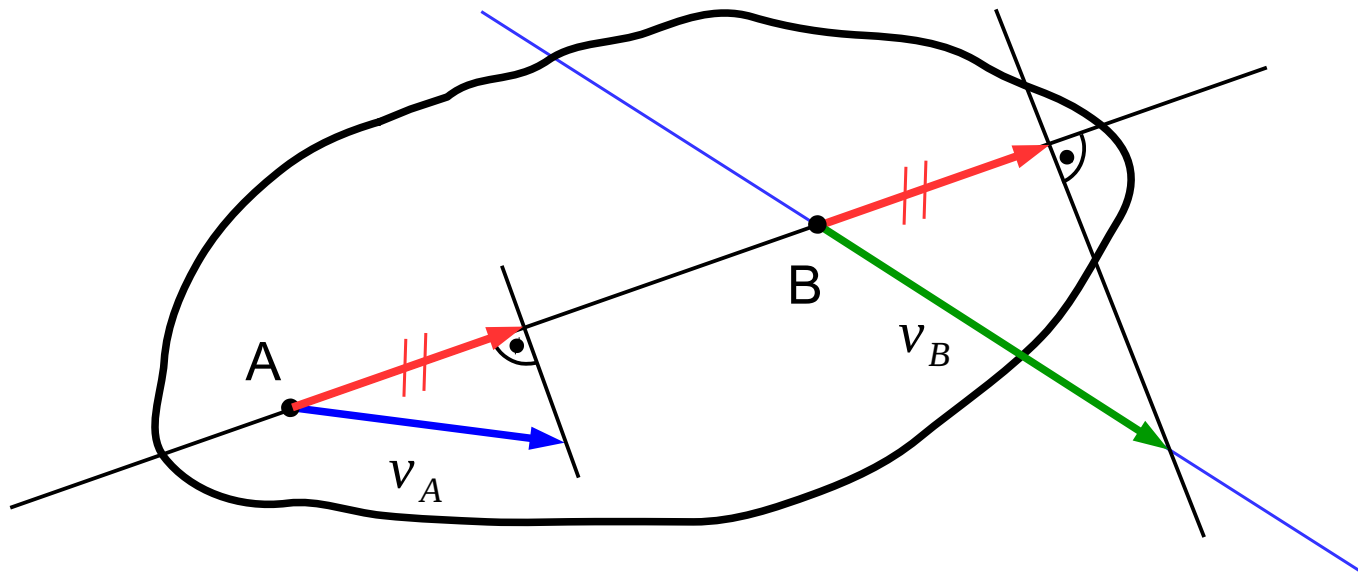


Velocity projection method

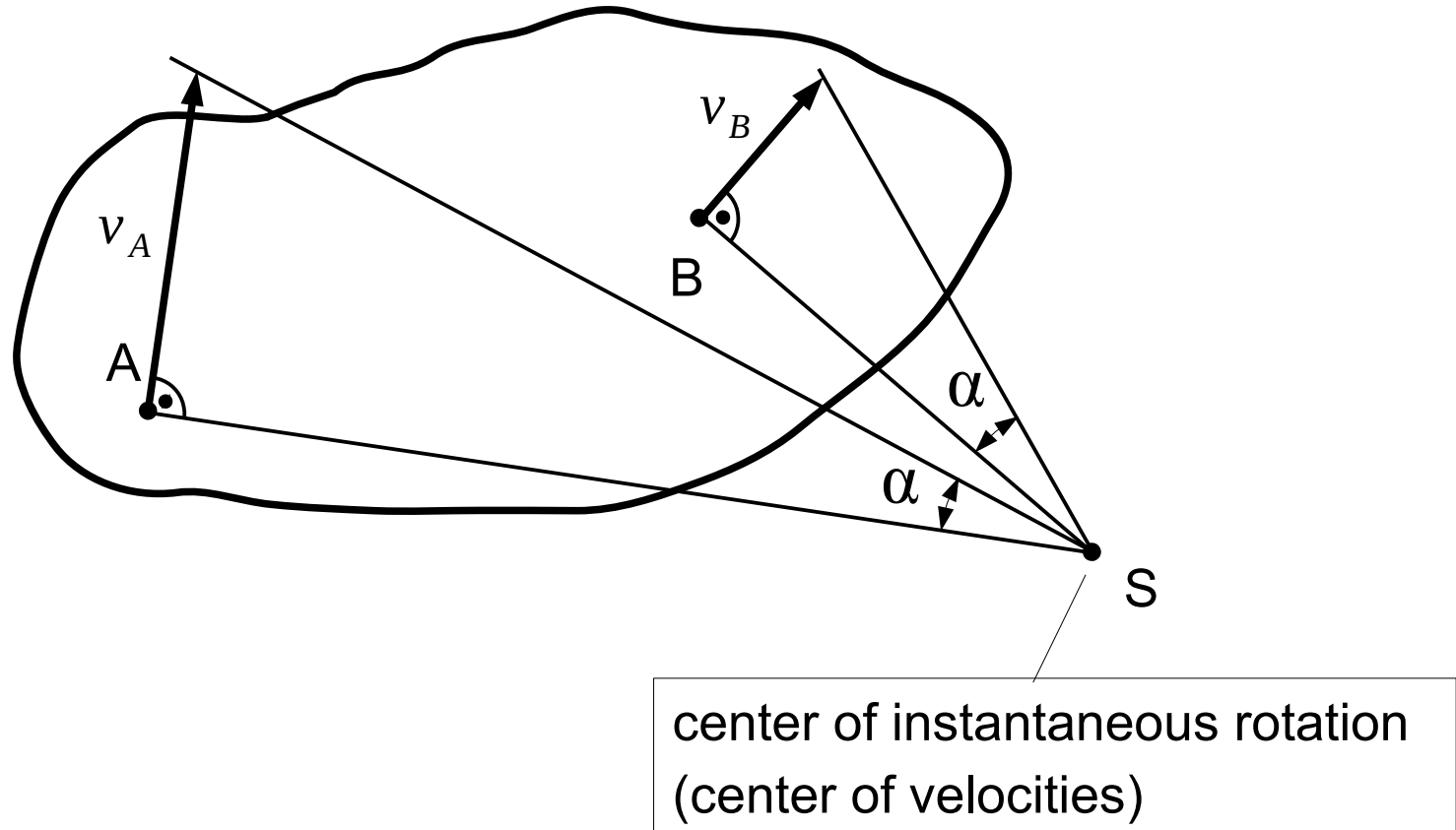
Example

Given: v_A and direction of v_B

Searched: v_B



Instantaneous center of rotation method

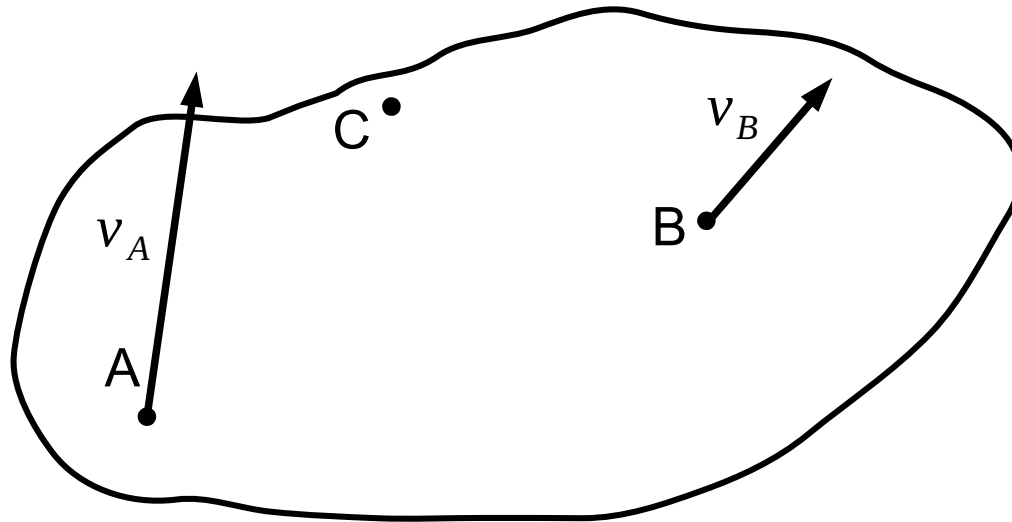


Instantaneous center of rotation method

Example

Given: v_A and v_B

Serched: v_C

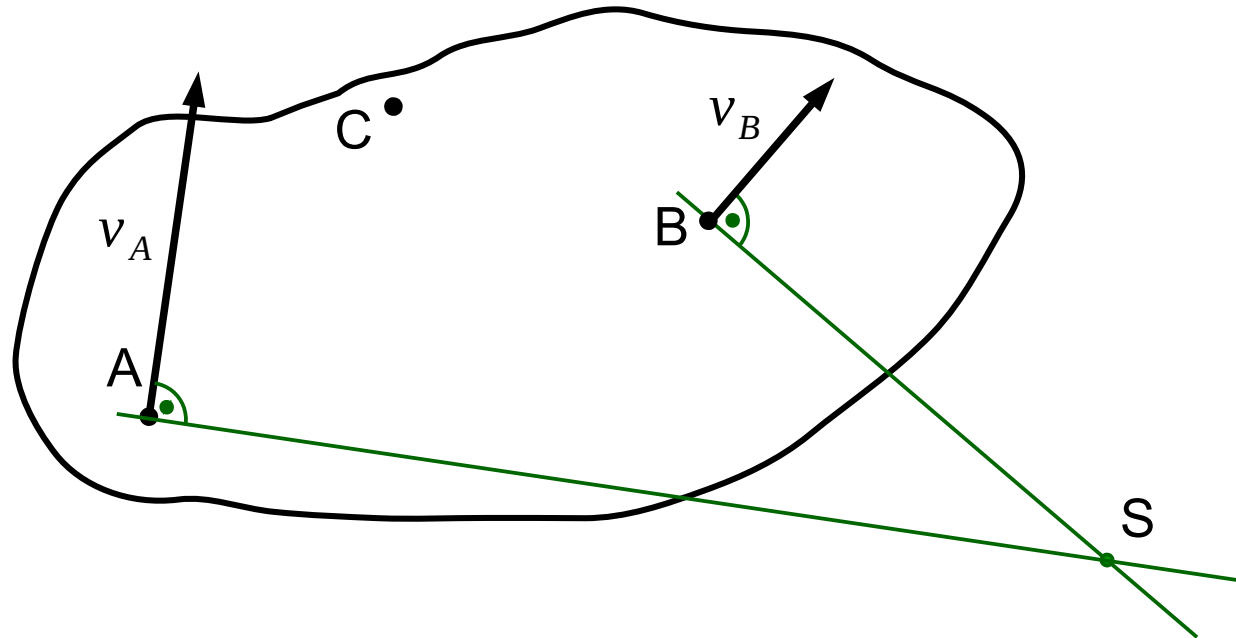


Instantaneous center of rotation method

Example

Given: v_A and v_B

Serched: v_C

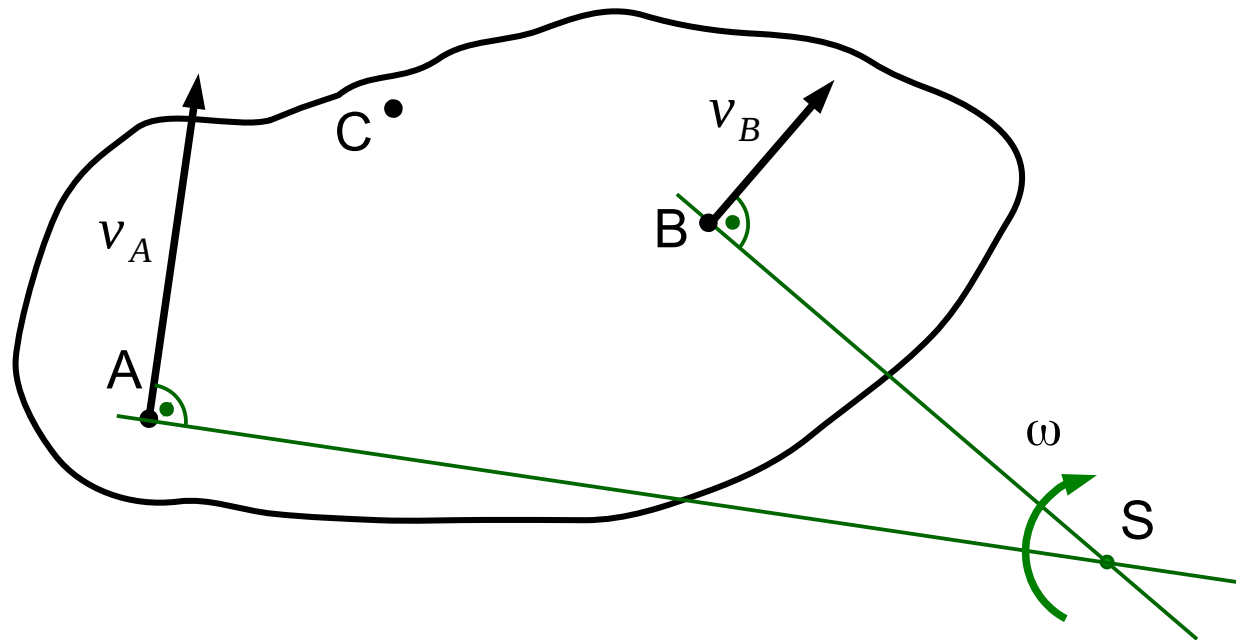


Instantaneous center of rotation method

Example

Given: v_A and v_B

Serched: v_C



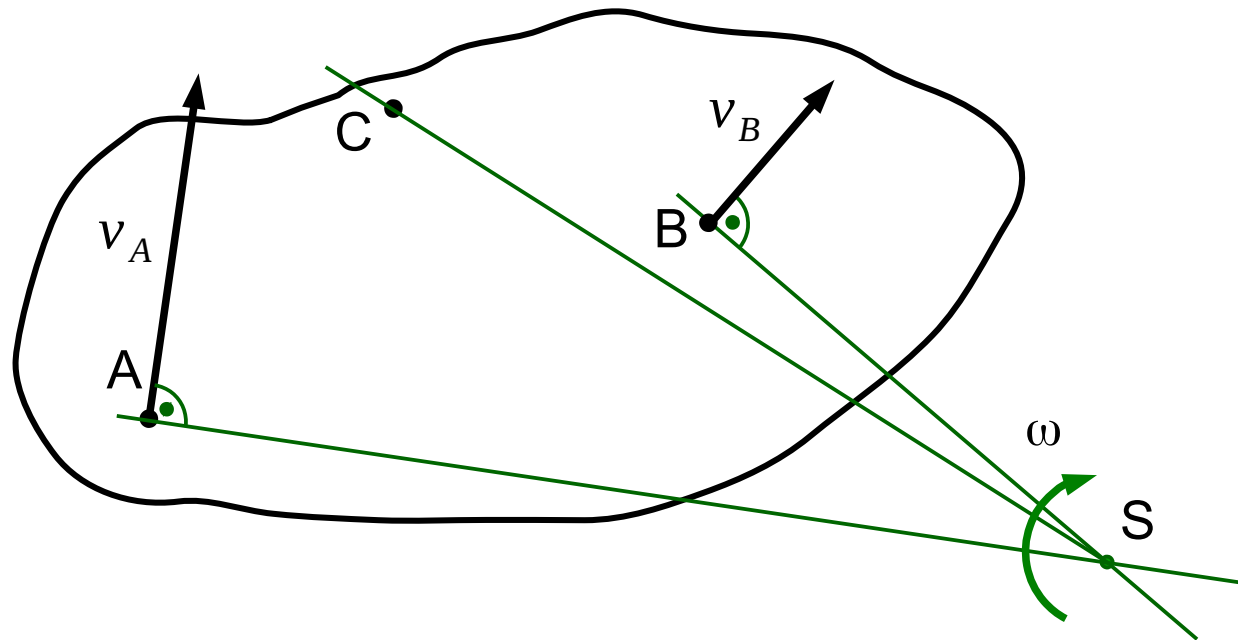
$$\omega = \frac{v_A}{|SA|} = \frac{v_B}{|SB|}$$

Instantaneous center of rotation method

Example

Given: v_A and v_B

Serched: v_C



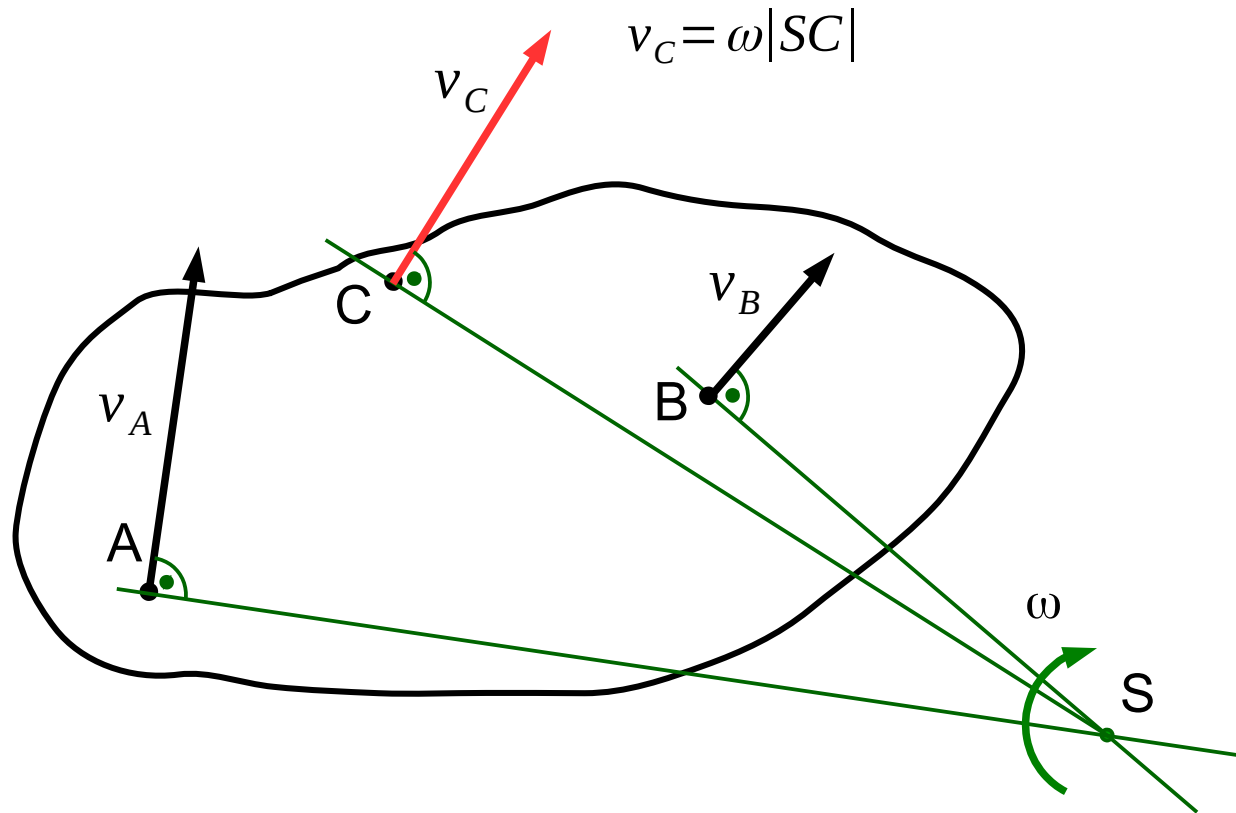
$$\omega = \frac{v_A}{|SA|} = \frac{v_B}{|SB|}$$

Instantaneous center of rotation method

Example

Given: v_A and v_B

Serched: v_C



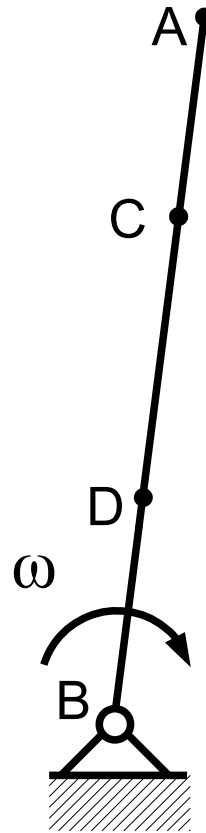
$$\omega = \frac{v_A}{|SA|} = \frac{v_B}{|SB|}$$

Instantaneous center of rotation method

Example

Given: ω

Serched: v_A, v_C, v_D

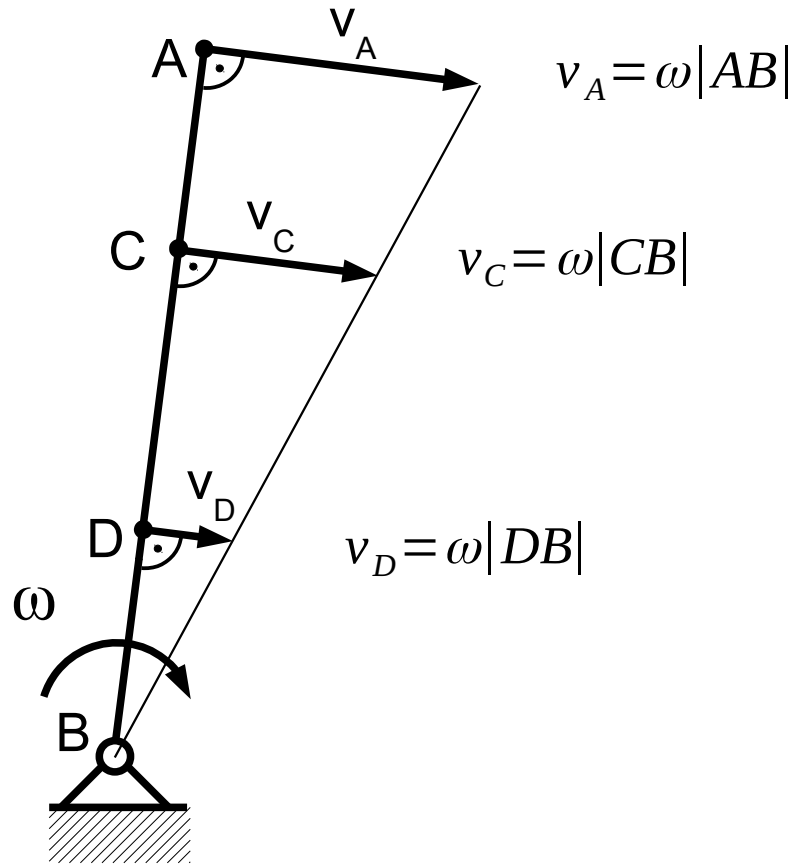


Instantaneous center of rotation method

Example

Given: ω

Serched: v_A, v_C, v_D



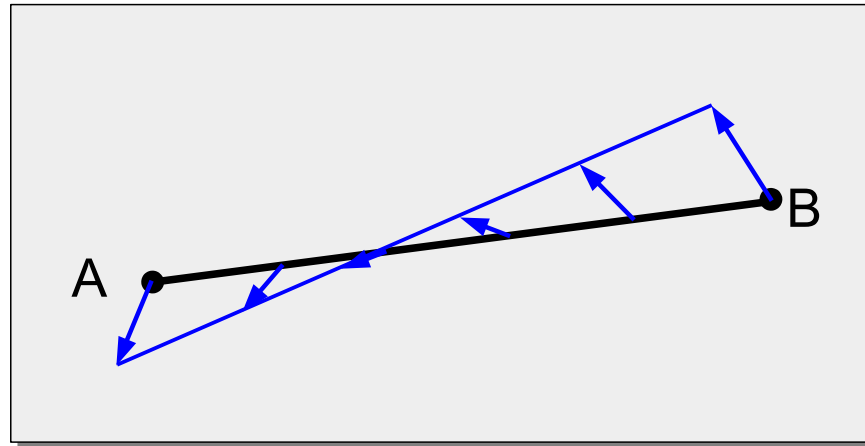
Velocity decomposition method

Every planar motion can be described by a superposition of a linear motion and an angular motion.

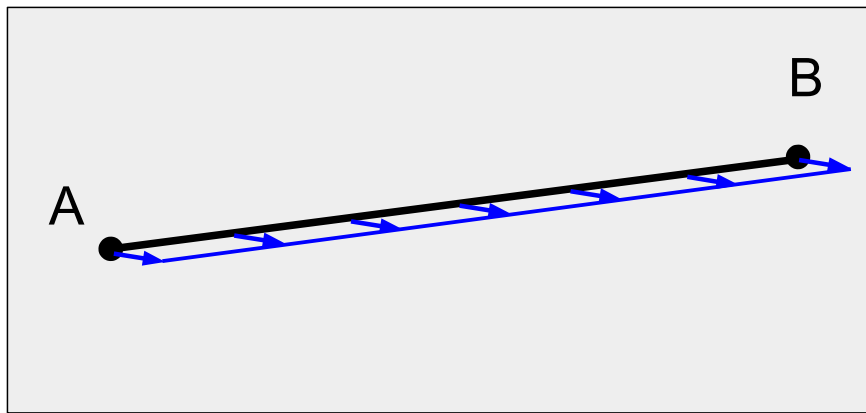
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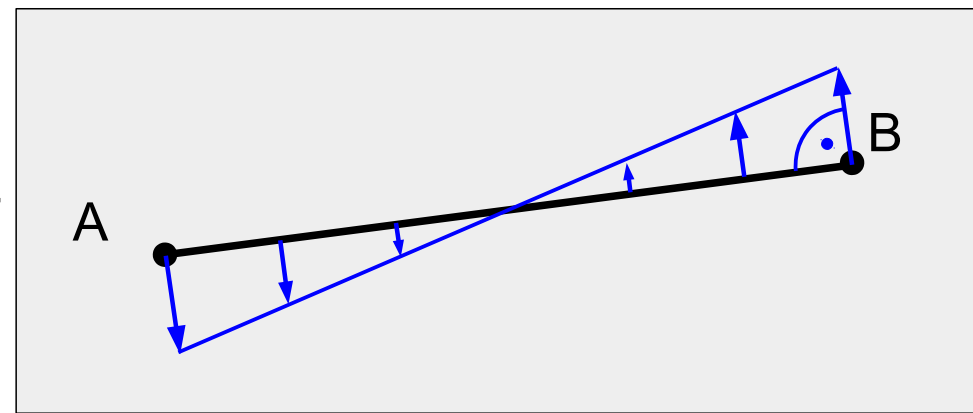
1st example



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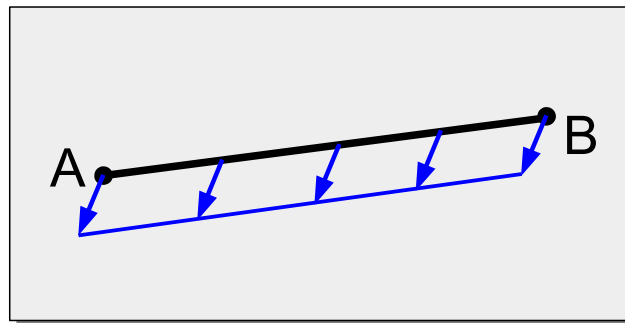
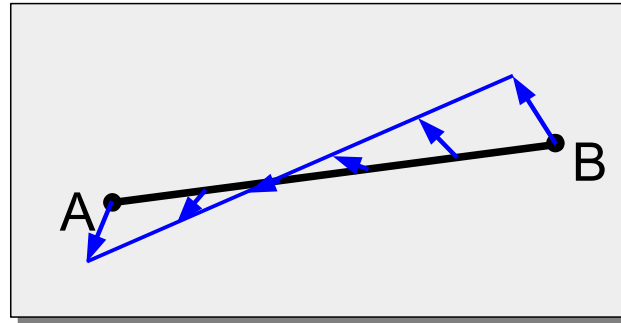


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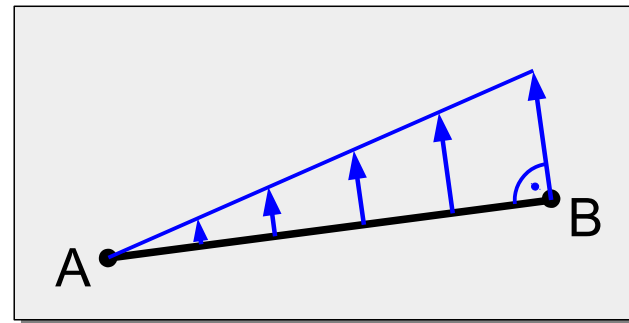


Velocity decomposition method

2nd example

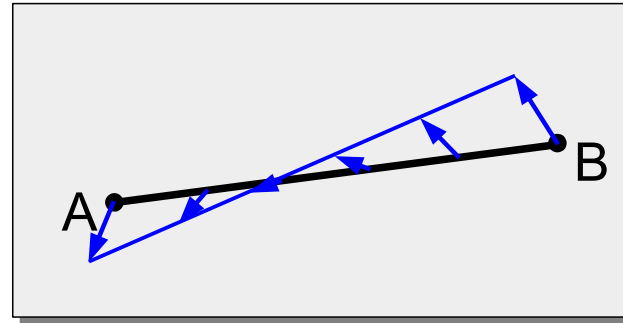


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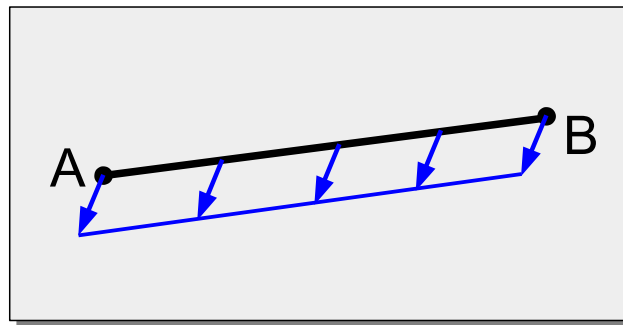


Velocity decomposition method

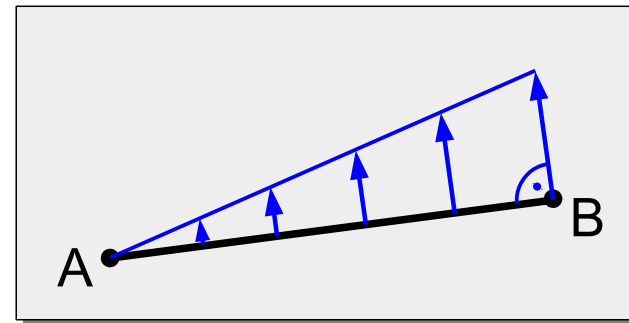
2nd example



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$$\vec{v}_B = \vec{v}_A + \vec{v}_{BA}$$

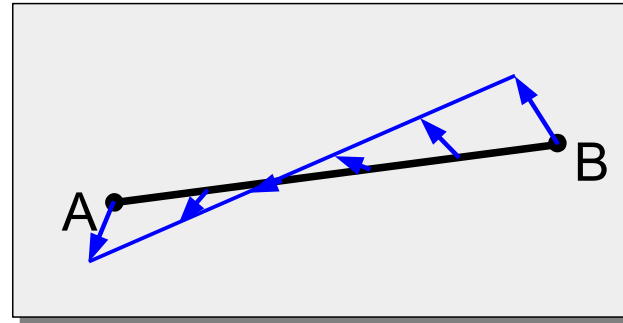
absolute velocity
of point B

velocity of a linear motion

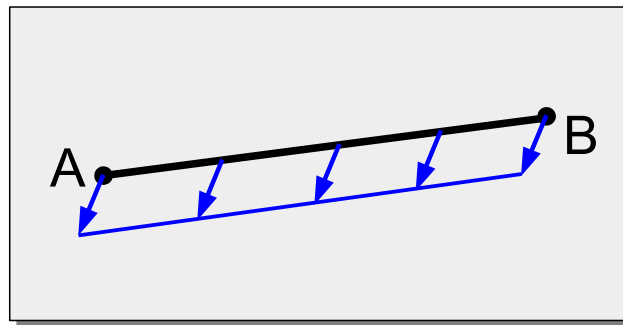
Angular velocity of point B
in rotation around point A.

Velocity decomposition method

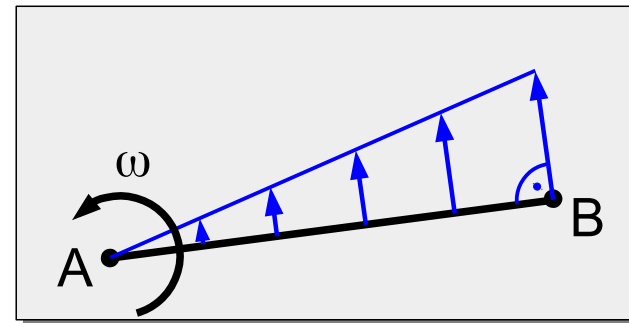
2nd example



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$$\vec{v}_B = \vec{v}_A + \vec{v}_{BA}$$

absolute velocity
of point B

velocity of a linear motion

Angular velocity of point B
in rotation around point A.

$$\vec{v}_{BA} = \vec{\omega} \times \vec{AB}$$

Velocity scheme method

Velocity scheme of a rigid body – geometry created by the ends of its velocity vectors moved to the common starting point (pole).

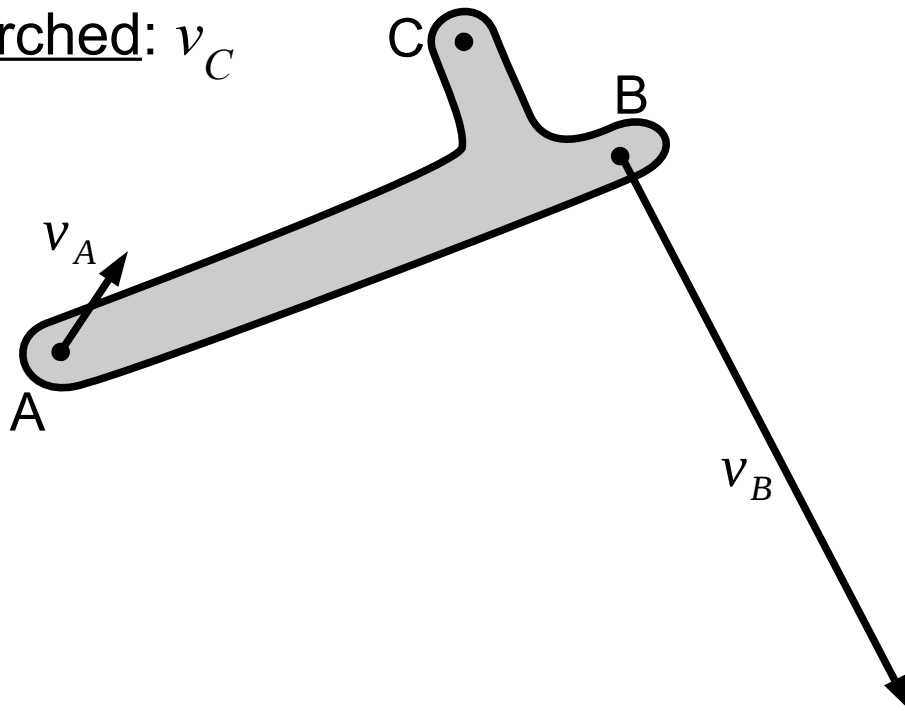
Velocity scheme is similar to the corresponding rigid body: it is scaled and rotated by an 90° angle in the direction of body's angular velocity.

Velocity scheme method

Example

Given: v_A and v_B

Serched: v_C

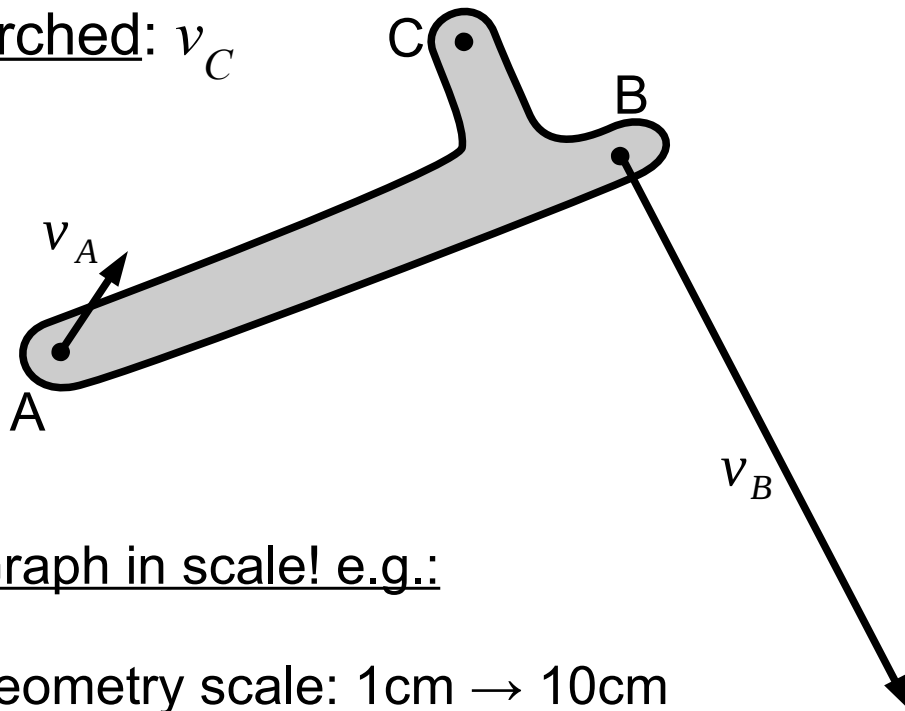


Velocity scheme method

Example

Given: v_A and v_B

Serched: v_C



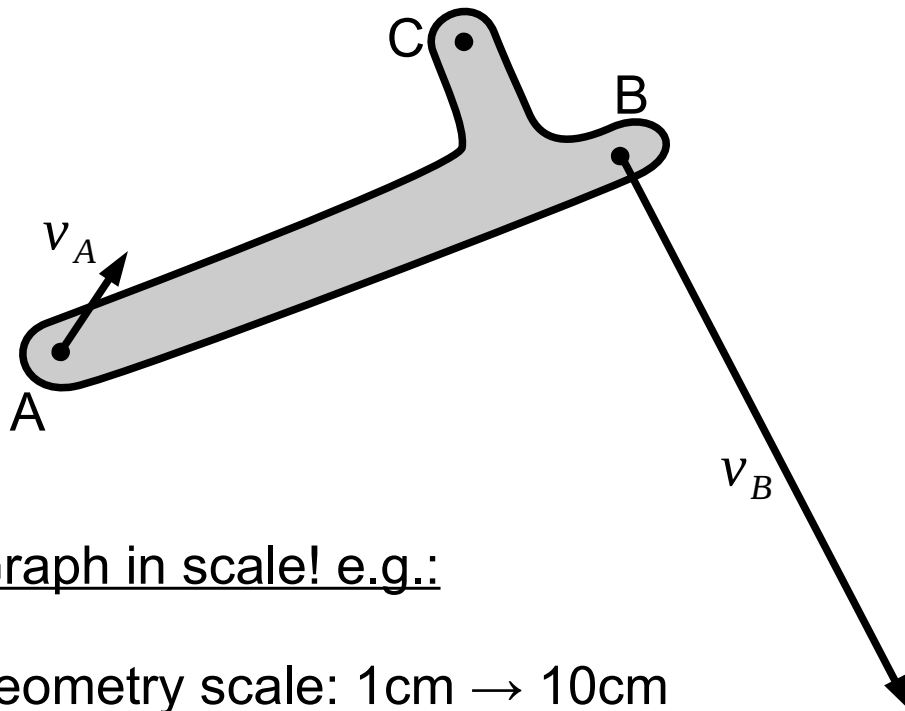
Graph in scale! e.g.:

geometry scale: 1cm \rightarrow 10cm

velocity scale: 1cm \rightarrow 1m/s

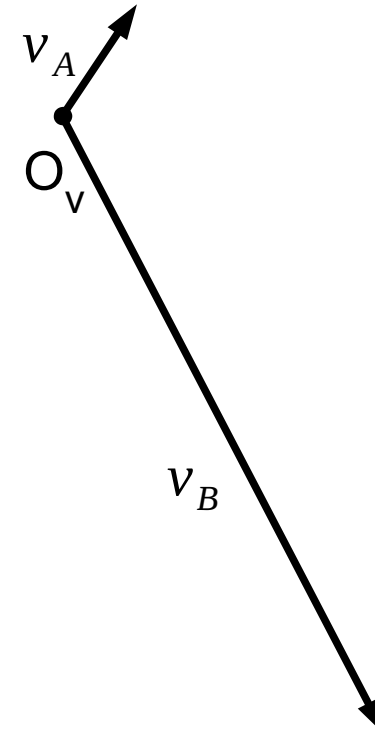
Velocity scheme method

Example



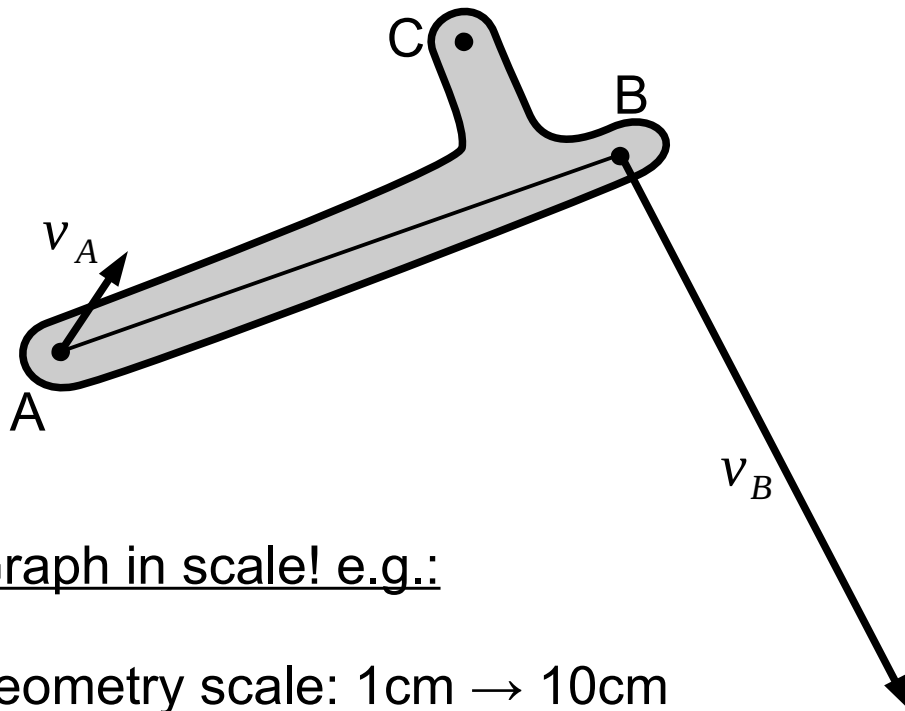
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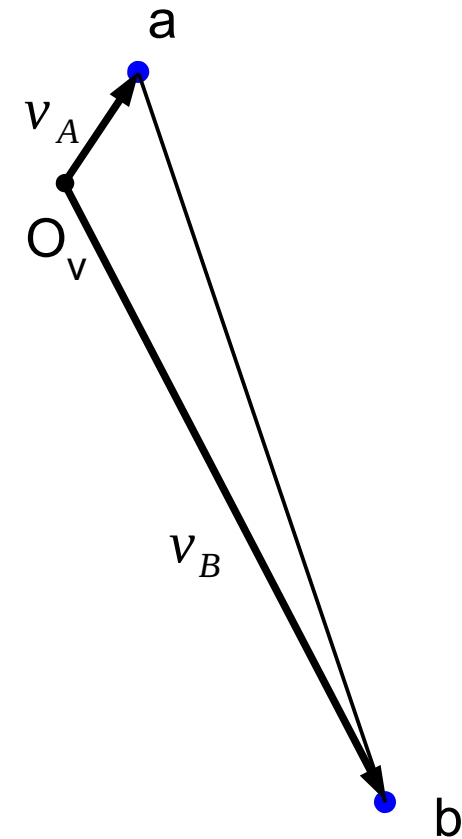
Velocity scheme method

Example



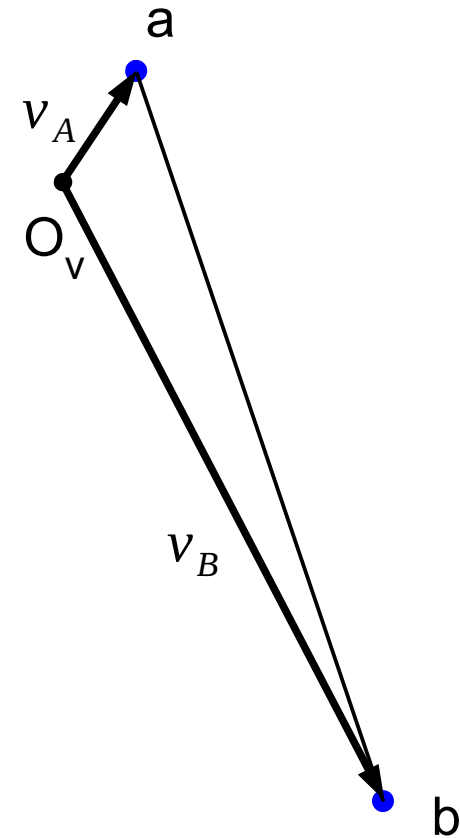
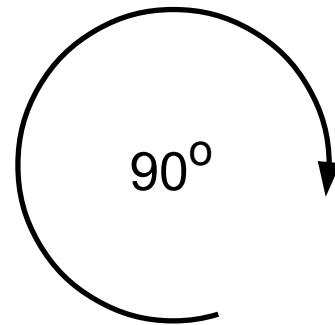
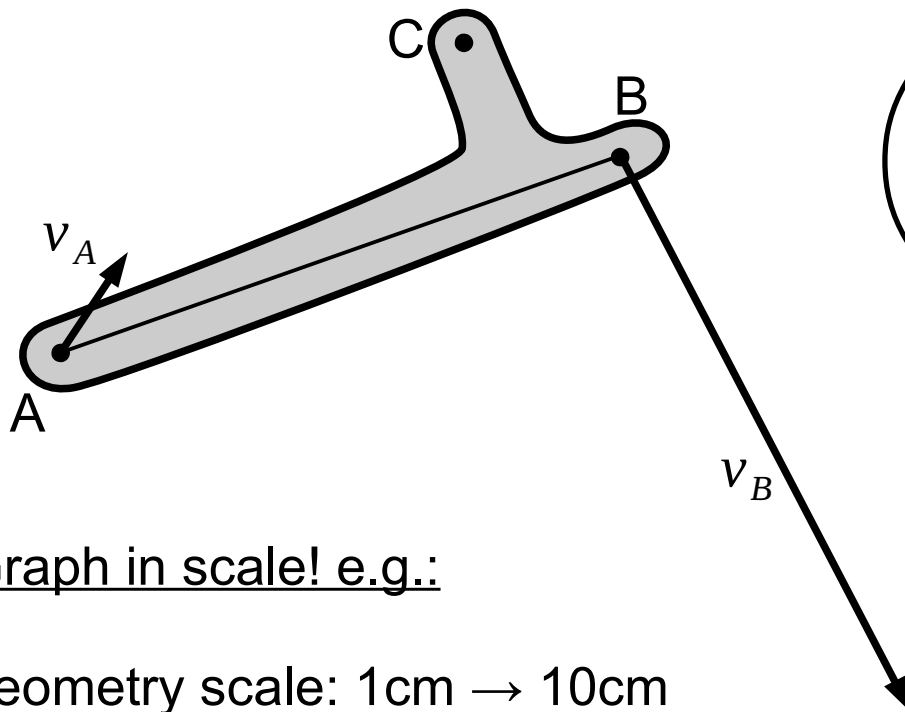
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Velocity scheme method

Example

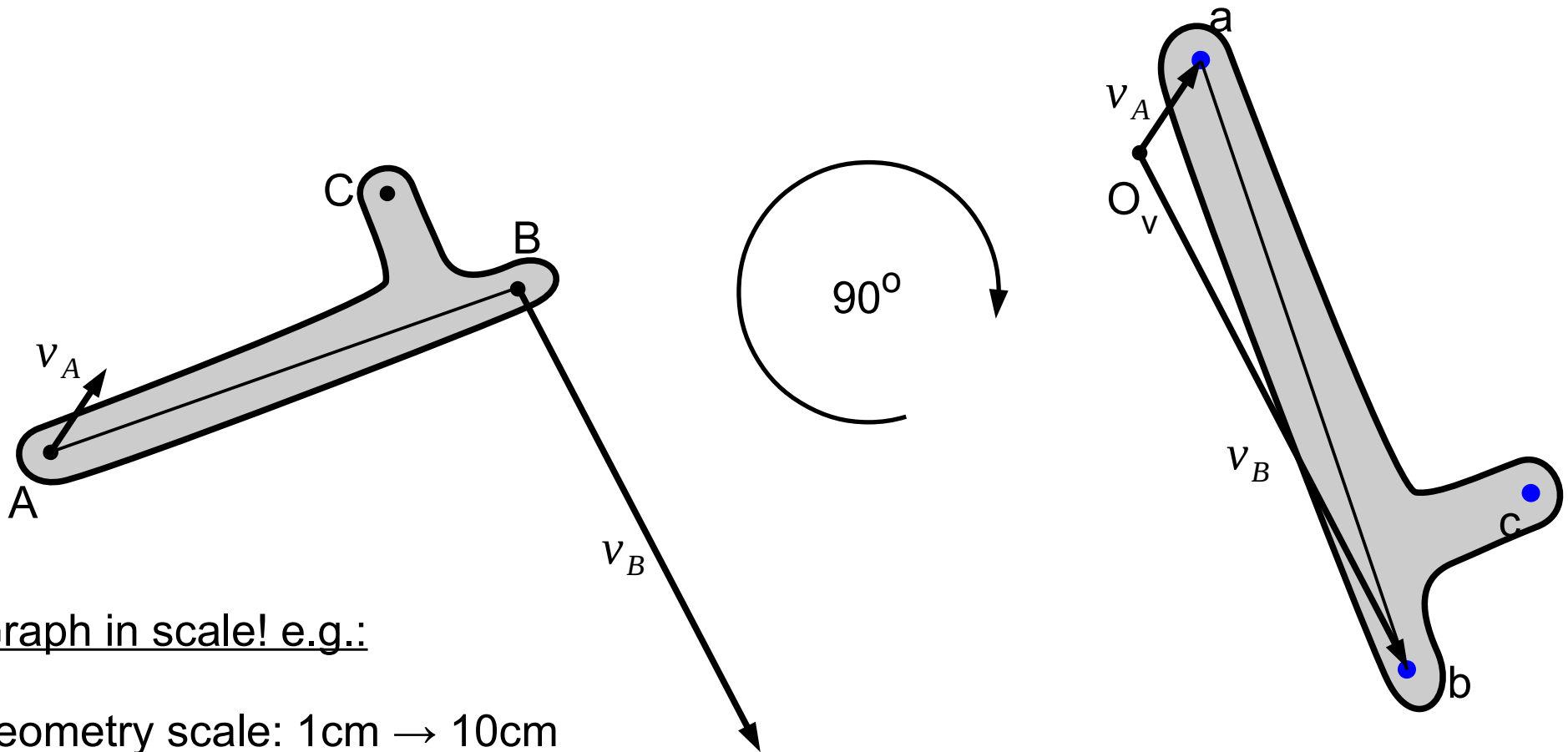


Graph in scale! e.g.:

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velocity scale: 1cm \rightarrow 1m/s

Velocity scheme method

Example



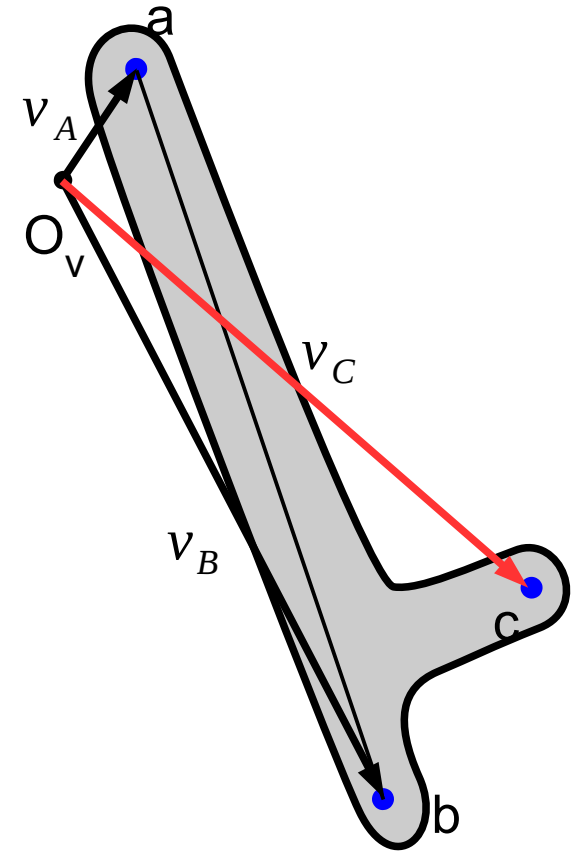
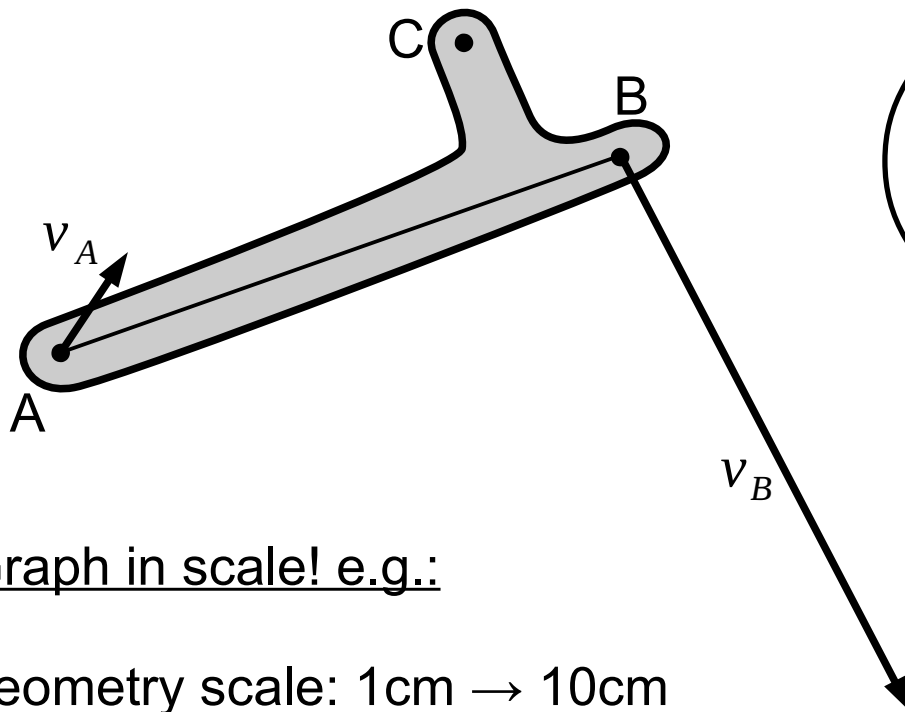
Graph in scale! e.g.:

geometry scale: 1cm \rightarrow 10cm

velocity scale: 1cm \rightarrow 1m/s

Velocity scheme method

Example

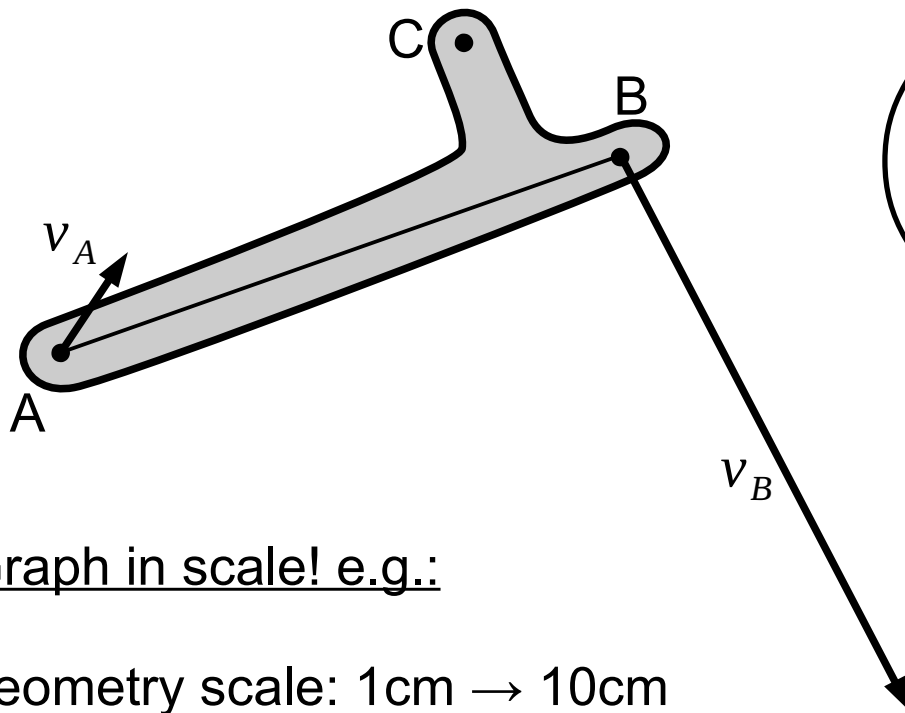


Graph in scale! e.g.:

geometry scale: 1cm \rightarrow 10cm
velocity scale: 1cm \rightarrow 1m/s

Velocity scheme method

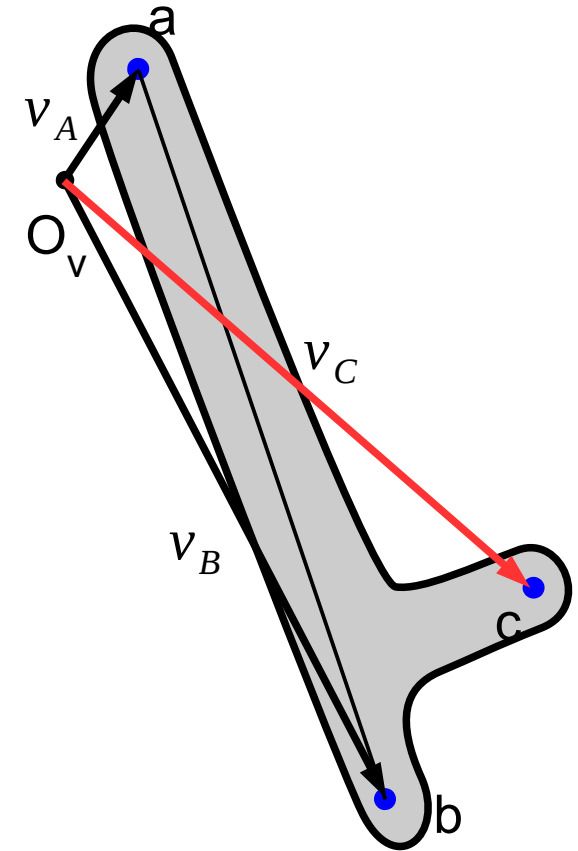
Example



Graph in scale! e.g.:

geometry scale: 1cm \rightarrow 10cm

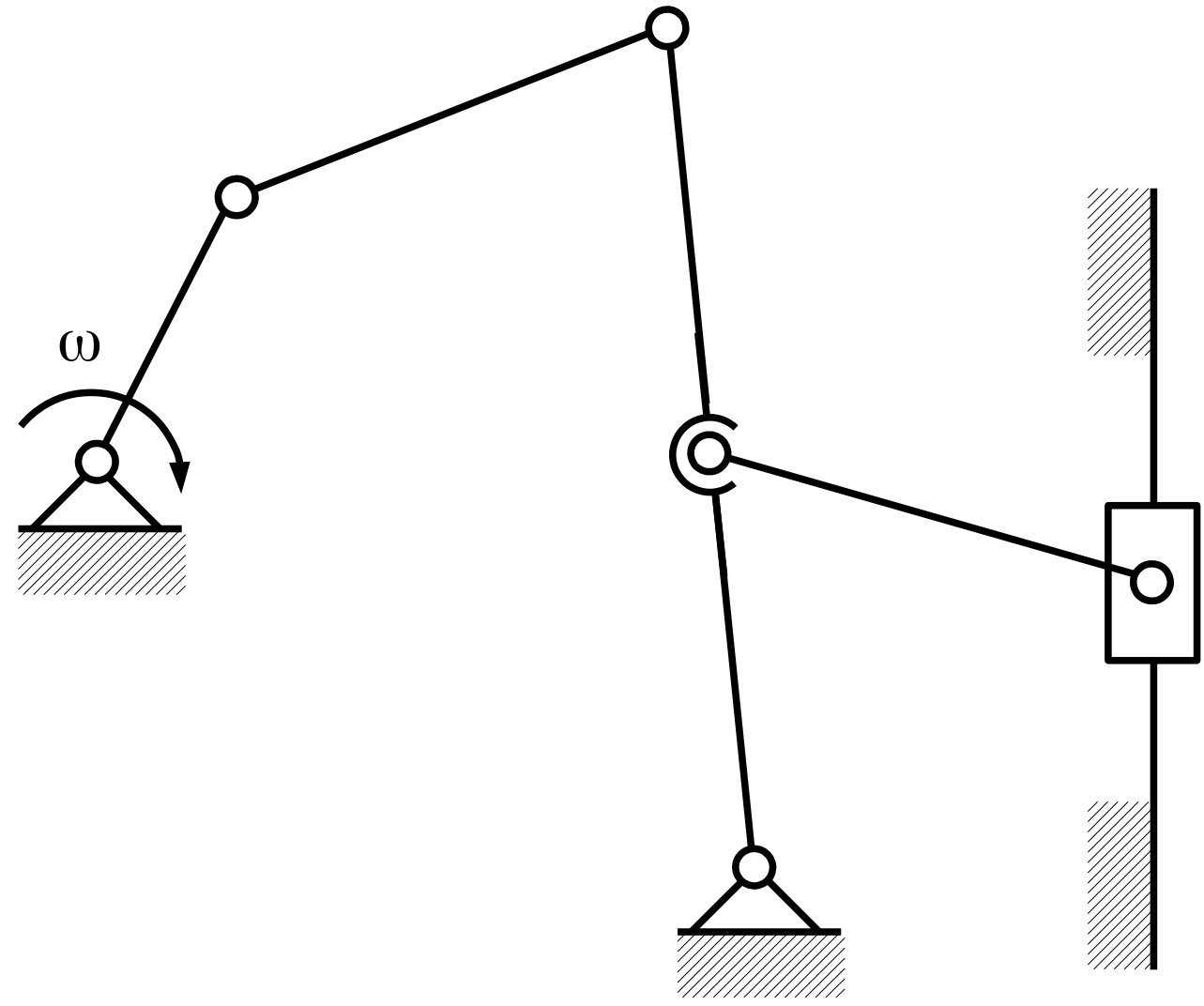
velocity scale: 1cm \rightarrow 1m/s



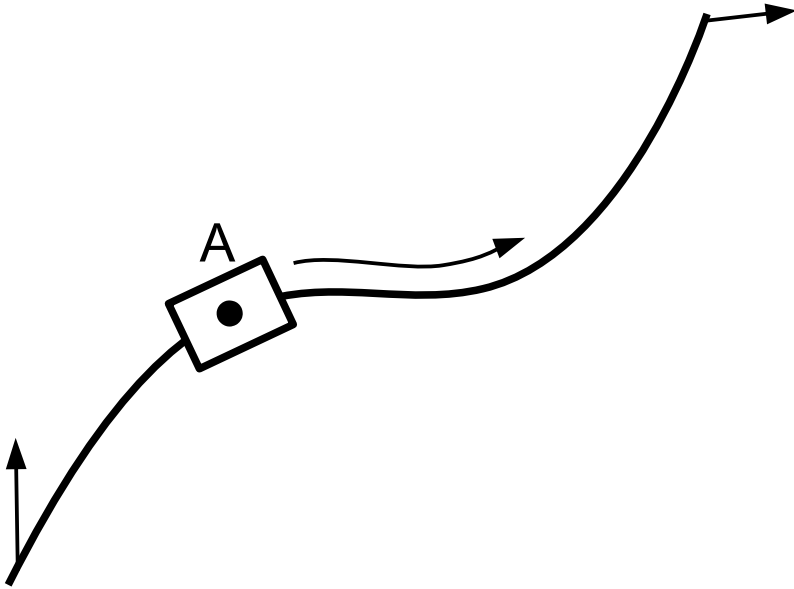
velocity scale: the same
geometry scale: new!

Velocity scheme method

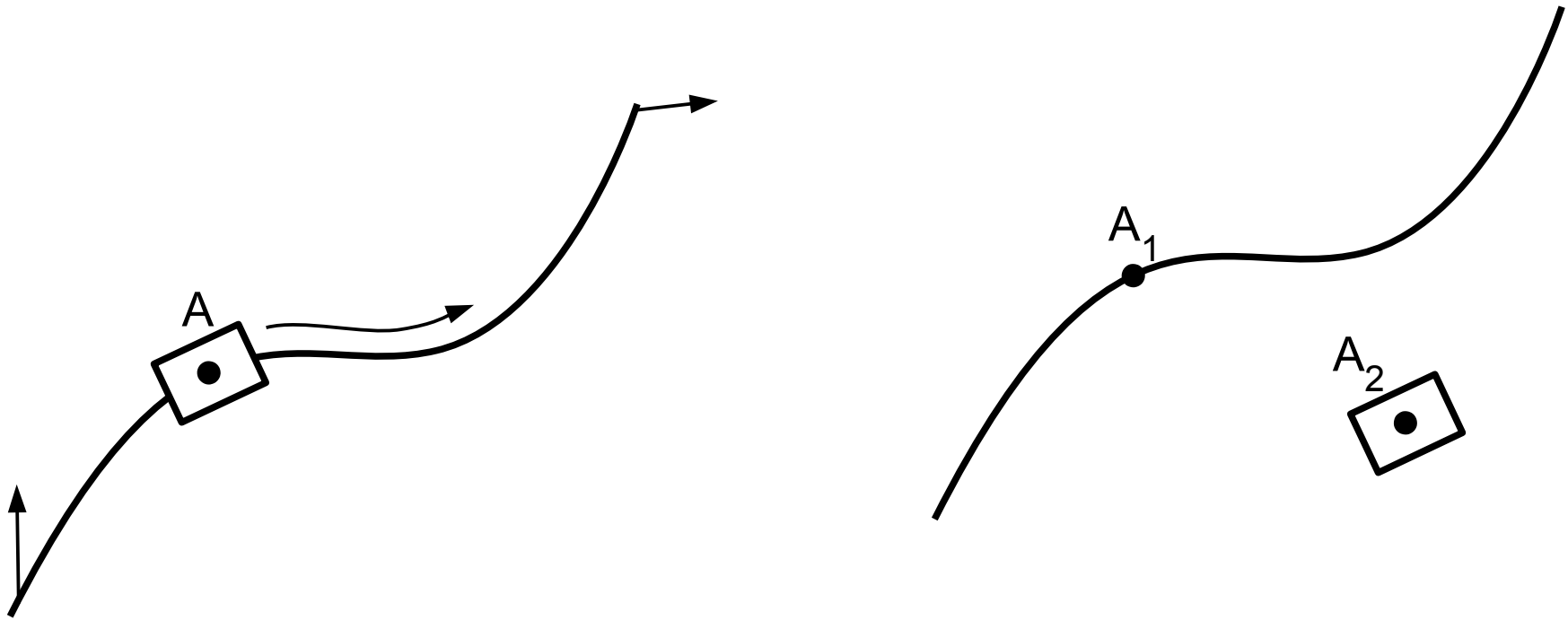
Example



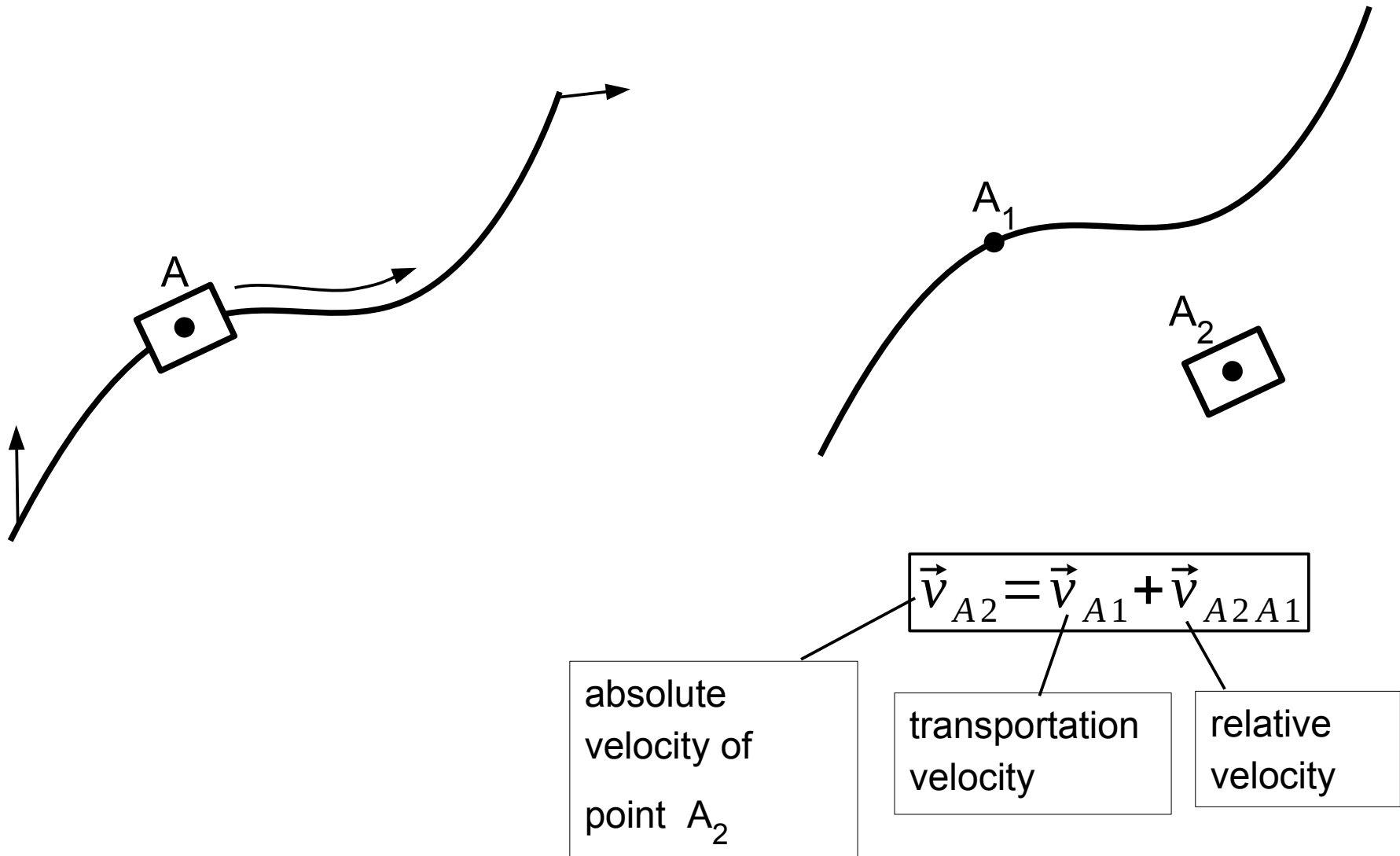
Velocities in relative motion



Velocities in relative motion



Velocities in relative motion



Velocities in relative motion

Example

